# A unified rough and finish cut algorithm for NC machining of free form pockets using a grid based approach 

Yong-hoon Yong-hoon<br>Iowa State University

Follow this and additional works at: https://lib.dr.iastate.edu/rtd
Part of the Engineering Commons

## Recommended Citation

Yong-hoon, Yong-hoon, "A unified rough and finish cut algorithm for NC machining of free form pockets using a grid based approach" (1999). Retrospective Theses and Dissertations. 17892.
https://lib.dr.iastate.edu/rtd/17892

# A unified rough and finish cut algorithm for NC machining of 

## free form pockets using a grid based approach

by

Yong-hoon Choi


#### Abstract

A thesis submitted to the graduate faculty in partial fulfillment of the requirements for the degree of MASTER OF SCIENCE


Major: Industrial Engineering Major Professor: Ranga Narayanaswami

Iowa State University
Ames, Iowa
1999

Copyright © Yong-hoon Choi, 1999. All rights reserved.

## Graduate College

## Iowa State University

This is to certify that the Master's thesis of Yong-hoon Choi
has met the thesis requirements of Iowa State University

## dedicated to

my father who is watching me in heaven and mother who always advises me positively

## TABLE OF CONTENTS

LIST OF FIGURES ..... v
ACKNOWLEDGEMENTS ..... vii
ABSTRACT ..... viii
CHAPTER 1. INTRODUCTION ..... 1
CHAPTER 2. RELEVANT LITERATURE ..... 6
CHAPTER 3. POCKET DEFINITION AND NAVIGATION ..... 12
3.1 Surface Definition ..... 12
3.2 Grid Definition ..... 13
3.3 Definition of Polygon ..... 16
3.4 Navigation Strategies ..... 17
3.5 Pocket Machining Algorithm ..... 21
CHAPTER 4. MACHINING PATH AND NC CODE GENERATION ..... 25
4.1 Line Movements ..... 25
4.2 Arc + Line Movements ..... 26
4.3 Bezier Curve + Line Movements ..... 29
4.4 Rough and Finish Cut ..... 33
4.5 Proposed Algorithm for Reverse Engineering ..... 34
CHAPTER 5. CASE STUDY ..... 37
5.1 General Polygon ..... 38
5.2 Rough and Finish Cut with Rectangle Pocket Shape ..... 38
5.3 Comments on Surface Error/Roughness/CL/CC ..... 39
CHAPTER 6. CONCLUSIONS ..... 49
APPENDIX. GENERATED G\&M CODES ..... 51
REFERENCES ..... 64

## LIST OF FIGURES

Figure 1. Staircase and Window-Frame Procedures ..... 2
Figure 2. NC Pocket Machining Algorithm ..... 5
Figure 3. A Representative Bezier Surface ..... 13
Figure 4. Digitization of Bottom and Tool Path Motion in XY View ..... 14
Figure 5. Possible Tool Moving Directions at Current Location ..... 15
Figure 6. Side View Corresponding to the Tool Path ..... 15
Figure 7. General Polygons with Convex and Concave Shape ..... 16
Figure 8. An Example of a Defined Polygon ..... 17
Figure 9. Checking Navigation Condition When Precedent Navigation ..... 18 was +X Direction
Figure 10. Checking Navigation Condition When Precedent Navigation ..... 19 was -X Direction
Figure 11. Checking Navigation Condition When Precedent Navigation ..... 19 was +Y Direction
Figure 12. Checking Navigation Condition When Precedent Navigation ..... 20 was -Y Direction
Figure 13. Flowchart for NC Pocketing ..... 23
Figure 14. Initial Preprocessing Procedure ..... 24
Figure 15. Linear Movements to Generate Curve ..... 25
Figure 16. Illustration of Arc + Line Movements ..... 27
Figure 17. Flowchart of the Arc/Line Segmentation Algorithm in XZ Plane ..... 28
Figure 18. Generation of Bezier Curve Tool Path ..... 30
Figure 19. Unit Distance in Bezier Curve ..... 31
Figure 20. Surface Point Error in Bezier Curve ..... 31
Figure 21. Bezier Curve + Line Movements Algorithm in XZ Plane ..... 32
Figure 22. An Example of Rough Cutting Steps in 2 Dimensions ..... 33
Figure 23. Proposed Reverse Engineering Algorithm ..... 35
Figure 24. An Example of Bottom Surface for Reverse Engineering ..... 35
Figure 25. Isometric and Top Views of the Main Tool Path ..... 40
Figure 26. Isometric and Top Views of the Pocket Wall Tool Path ..... 41
Figure 27. Intermediate and Full Processing of X zigzag Tool Path ..... 42
Figure 28. Intermediate and Full Processing of Y zigzag Tool Path ..... 43
Figure 29. Real Machining Samples ..... 44
Figure 30. Isometric and Top Views of Final Result after Main, Wall, X and ..... 45 Y zigzag Tool Path
Figure 31. Arc + Line Movements on the Same Polygon ..... 46
Figure 32. Bezier Curve + Line Movements on the Same Polygon ..... 46
Figure 33. $1^{\text {st }}, 2^{\text {nd }}$, and $3^{\text {rd }}$ layers of Rough \& Finish Cut ..... 47
Figure 34. $4^{\text {th }}, 5^{\text {th }}$, and Final Layers of Rough \& Finish Cut ..... 47
Figure 35. Relation of CL, CC, and Surface Error ..... 48

## ACKNOWLEDGEMENTS

So far, I have received a lot of encouragement and valuable friendship from a number of people. First of all, I would like to show my sincere gratitude to my major professor, Dr. Ranga Narayanaswami for his friendly and supportive help, my thesis committee members, Dr. Thomas Barta and Dr. Shyam Bahadur for their valuable advice.

This thesis is also done with a great help from my senior, Chiwoon Cho who gave me excellent guidance throughout the work. I also would like to thank Dr. Theodore H. Okiishi for his good advice.

Finally, I appreciate the love and support of my dear mother with all my heart and thank all my teachers and friends whose names are too numerous to list here.

## ABSTRACT

Determination of tool cutter path in an efficient manner is very important to generate final NC codes for machining. This is particularly true for machining general pockets with sculptured surfaces on a three-axis CNC milling machine. A machined surface is judged by the surface roughness, accuracy of machined features and by the total machining time.

Many CAD/CAM systems use linear interpolation to generate numerical control tool paths for a curved surface. However, this needs to be modified to improve the smoothness of the machined surface and to reduce machining time. This is because linear interpolation has limitations such as larger values of surface roughness and accuracy, more machining time because of repeated 'stop \& go' motions and large cutter location data files.

Curved machining can be a solution to reduce these problems. In this thesis, an analytical procedure for generating a final NC program based on linear interpolation and a combination of linear and curvilinear interpolation is presented. The algorithm for tool path determination allows for motion along a line, circular arcs and Bezier curves.

The tool path is planned using a navigation algorithm on a surface discretized using an appropriate grid size. The navigation strategy is to move the tool from one grid point to the next in an efficient manner so that a valid coverage of the bottom surface of the pocket is produced. X and Y zigzag motion commands are additionally added to minimize the surface roughness. The entire tool path consists of interior navigation amidst the grid points; machining along the wall periphery and zigzag motion commands. Deep pockets are handled
by extending the algorithms with a layered machining approach. Rough machining is performed in several layers and the last layer is the finish cut.

The algorithm works for any general pocket with arbitrary wall geometry and freeform bottom surface. The bottom surface can be represented by any analytical or parametric surface or can be grid data from reverse engineering. The grid-based approach allows the application of suitable curvilinear interpolation algorithms for high fidelity machining. The algorithm is validated by graphical simulations in OpenGL as well as by machining experiments.

## CHAPTER 1. INTRODUCTION

With increased demand for complicated form and functional surface shape in many industrial products, there is a distinct need for efficient CNC (computer numerical controlled) machining of compound-curved and intricate surfaces. One of the most important features in determining CNC machining efficiency and productivity is cutter path motion. This cutter motion on compound-curvature surfaces determines the machining time and the surface roughness. Surface roughness always exists because of the lack of geometry matching between cutter and the surface to be machined. The major problem in generating automatic ball end milling cutter paths is the difficulty of determining the cutter path for general polygons with compound-curvature surfaces.

Generally two strategies have been used, namely, Staircase and Window-frame. In the staircase pattern the tool is moved along parallel line segments in a chosen direction. In the window-frame technique the cutter path is a spiral obtained by offset from the wall boundary. Figure 1 shows both the staircase and window-frame techniques. These techniques are easy to implement for convex polygons with flat bottoms, but are quite difficult when the polygons are non-convex and have sculptured bottoms.

Most CAD/CAM systems machine curved surfaces by an approximation using linear interpolation. This method creates many short linear move commands with sudden changes in direction. Further, a lot of data points are needed to specify the tool size and this can result in prohibitively large cutter location file sizes. Moreover, machining with linear segments contributes to significantly larger values of surface roughness because of interpolation
approximation errors and considerably longer machining times due to repeated 'stop and go' tool motion.

Curved bottom machining algorithms with real curvilinear interpolation strategies are needed for efficient pocket machining. Cutter location file sizes also need to be reduced, so that complex-curved surfaces can be efficiently machined. This is becoming increasingly more relevant today with the common practice or desire for distributed design and manufacture. With curvilinear machining algorithms the cutter location file size can be significantly reduced because for machining the same amount of volume, curved data only needs starting and ending points and arc center or intermediate control points while linear movements need all data points to show the tool path.

a) Staircase Procedure

b) Window-frame Procedure

Figure 1. Staircase and Window-Frame Procedures

In view of the deficiencies mentioned above, the primary objective of this thesis is to develop an algorithm for machining freeform pockets with arbitrary wall geometry using a combination of linear and curvilinear interpolation strategies. The window-frame technique augmented with a grid-based navigation technique is used. The freeform pocket surface is
discretized into set of 3D XYZ data points. The number of points obtained is dependent on the grid size, which in turn is related to the diameter of the end mill. The navigation algorithm plans tool motion from the center of each grid element to the next one. The motion starts from one of the edges of the polygon and continues in a counter-clockwise direction whenever it reaches a pocket wall. The navigation algorithm is a search procedure that ensures valid coverage of the pocket. The searching process stops somewhere near the center of the polygon. This essentially makes up the tool path for the interior of the pocket. To this, extra X and Y zigzag motion commands are added to improve the surface roughness. This is particularly important here because of the freeform bottom pocket surface. The periphery of the pocket wall is then subsequently obtained by connecting a set of corner points that are determined as an offset from the vertices of the polygon defining the pocket. The interior cutter motion is actually reversed for physical machining of the pocket as this procedure reduces the tool moving time for subsequent wall machining.

The motion along the grid center points can then be post processed for implementing curvilinear machining algorithms. A circular arc-machining algorithm is implemented to improve the surface roughness, reduce machining time, and cutter location file size. To remove the same amount of volume compared to line movements, arc-machining only requires specifying the start point, end point, and arc radius. A series of data points are approximated by an arc which passes through the start point, the end point and the middle point. The user can specify a suitable tolerance value for the error between the arc and the grid data points. If the error is within the tolerance, then this arc is accepted and the next data points are considered. If not, the data point set is reduced by one and the process is repeated.

Bezier curve path is another approach. This method requires the specification of start and end points as well as intermediate control points. Since the first and last control points are the same as start and end points, only intermediate control points need to be found with given information. To define a cubic Bezier curve at least four known points on the curve are needed. These are the start and end points and two intermediate points. If the number of data points is less than four, then linear interpolation is used. Depending on the polygon shape, this approach might be useful.

To handle the machining of deep pockets, a layer based machining strategy is used. Material is removed layer by layer. The navigation algorithm is essentially the same but is used repeatedly in layers. For this search, the algorithm is termed as a "unified rough and finish cut" algorithm. The algorithm allows the user to choose unit depth step at each layer. If curvature at a certain layer is steep relatively to the other layer, the unit depth of that layer can be modified flexibly.

The algorithm can be extended to machine pockets that are reverse-engineered. This is particularly simple because the algorithm is based on a grid-based approach and the points that are measured are essentially the grid points.

The entire pocket-machining algorithm is illustrated schematically in Figure 2 and can be stated as follows:

1) The bottom surface and polygon shape of pocket are defined.
2) Main interior, wall machining, $X$ zigzag, and $Y$ zigzag tool paths are determined in navigation stage
3) Tool path motion is obtained in terms of line, arc + line, and Bezier curve + line movements as desired



Figure 2. NC Pocket Machining Algorithm

The rest of the thesis is organized as follows. Relevant literature is introduced in Chapter 2. Chapter 3 describes the definition of the pocket in terms of the bottom surface of the pocket using grids and the polygon defining the walls. The grids are specified by the user in relation to the tool diameter. The navigation strategies with all possible cases are also described in Chapter 3. Machining path determination and NC code generation which may comprise of line, arc + line, and Bezier curve + line movements are shown in the first half of Chapter 4. Rough and finish cut and reverse engineering methods are introduced in the second half of Chapter 4. Case studies are clearly shown by simulations and machining experiments in Chapter 5. Finally, conclusions are presented in Chapter 6.

## CHAPTER 2. RELEVANT LITERATURE

CAPP (computer aided process planning) is considered as one of the most important steps in converting a design concept into a manufactured product. The introduction of CAPP has certainly made the planning function more efficient. According to Houtzeel (1995), there are three general basic principles for CAPP. These are variant, generative, and automatic process planning.

The variant approach to process planning is to create a new plan for a new part by recalling, identifying and retrieving an existing plan for a similar part. A set of standard process plans is established for all the part families identified through GT (group technology). When a new plan is required, the most closely matching standard plan is retrieved and edited to suit the specific requirements of the new part. Variant process planning systems are relatively easy to build and complicated activities and decisions require less time and labor. This approach is still popular even though experienced process planners are required to adjust the standard plan.

The generative approach to process planning is to generate a new plan automatically by means of decision rules, algorithms and geometry based data to perform uniquely many processing decisions from converting a part from raw material to a finished part. An attempt is made to synthesize each individual part using appropriate algorithms that define the various technological decisions that must be made in the course of manufacturing. In a truly generative system, unlike the variant approach, the sequence of operations as well as all the process parameters would be established automatically, without reference to prior plans.

Automatic process planning can generate a complete process plan directly from an engineering design model. The major goal of the automatic approach is to have the ability to generate a process plan for manufacturing parts automatically using no human input except the computer databases that contain the required information. The major difference between an automatic approach and other approaches is the CAD interface to extract for manufacturing.

Lee and Chang (1995) proposed to apply computational geometry techniques in process planning and optimizing the machining of complex surfaces. Polygon decomposition techniques and convex hulls were used to interrogate the surface and facilitate automatic process planning for machining complex surfaces. The concept of Group Technology (GT) was adopted to classify surfaces into different categories to assist in selecting machining operations. An operation plan was generated based on the geometric information extracted from the surface description arising from surface interrogation. Techniques have been proposed in this paper to optimize tool selection and cutter path generation of 2.5 D surface pocketing to improve machining productivity.

Different types of tool path planning strategies have been developed to generate a free form surface. These include iso-parametric machining, adaptive iso-curve machining, and pocketing with window frame or staircase style.

By using iso-parametric curves as tool paths, costly surface-surface intersection computations can be avoided. Iso-curvature machining was proposed due to the advantages it offers in terms of local placement and orientation of the tool. However the spacing between iso-parametric lines, in general, will be non-uniform causing overmachining or undermachining. And also the difficulties associated with the computation of lines of curvature
are the disadvantages of this approach (Sarma and Dutta 1997). Another problem with isoparametric curves is that tool paths do not provide an optimal coverage of the surface. Some areas may be overmachined because of redundancy. Elber and Cohen (1994) developed an adaptive sub-isocurve extraction approach that provided more optimal and valid coverage of the surface by adaptively introducing partial sub-isocurves.

Yang and Kong (1994) performed a comparative study of linear interpolators and parametric interpolators used for command generation for CNC machining. They found that the linear interpolator has the advantage of simplicity, and requires less computation while the parametric interpolator is superior in terms of its memory-size requirement, speed, accuracy, and so forth.

The ultimate goal of pocket machining is the automated generation of correct and optimal tool paths. Held (1994) classifies pocket-machining algorithms broadly into two categories. These are contour-parallel machining and direction-parallel machining. Contourparallel machining uses offset segments of the boundary elements of the pocket as tool path segments (window frame approach). Thus the pocket is machined spirally by the tool(s) being driven along the boundary offset that is at constant distances from the pocket's boundary. So this strategy is also known as offset machining. In directional-parallel machining (staircase style), the tool(s) is moved along line segments, which is parallel to a reference line selected initially. On the basis of this strategy, a connected tool path is obtained by linking these parallel segments such that they are either all traversed from right to left (or from left to right), or alternatively from left to right and from right to left. Held proposed an approach to the efficient generation of tool paths for pocketing based on 'proximity maps' and is basically contour-parallel machining.

Wang et al. (1988) proposed an approach to optimize NC tool path planning for flat face milling. A mathematical model was formulated and a solution procedure for calculating an optimal length of cut for a triangle was made for a convex shaped polygon.

Recently, Voronoi diagrams have been used in pocketing machining. Jeong and Kim (1998) developed a Voronoi diagram of a pocket to partitions regions inside the pocket. In this scheme, each region, called a Voronoi polygon, contains the set of points that are closer to the associated curve segment than to the others in the pocket boundary.

Sarma and Dutta's (1997) tool path generation method requires the surface data and tool radius as input. Their premise was that geometry and spacing of the tool paths impact scallop height and manufacturing time respectively. So they worked towards controlling the scallop height of the manufactured surface by modifying the tool path. They used offsets of the design surface to generate the tool path with the objective of obtaining a constant scallop height. According to Maeng, Ly, and Vickers (1996), the best geometry match between cutter and surface is obtained when the cutter is moved along the lines of the steepest surface slope.

Lynch (1996) states that more and more companies are finding it necessary to machine complex three-dimensional shapes. With the increasing availability of excellent and relatively easy-to-use computer-aided manufacturing (CAM) systems, this trend toward machining complex shapes on CNC machining centers will continue well into the foreseeable future. Based on the shape to be machined, the CAM system will generate a series of very tiny movements, usually straight-line G01 movement, which will form the shape being machined. In essence, the CAM system will do its best to interpolate the shape being machined based on an interpolation resolution. This resolution determines how accurately the
workpiece will be machined, and how long the CNC program will be. The tighter this resolution, the better the work-piece accuracy, but the longer the CNC program.

Beard (1997) states that the linear interpolation paradigm has come to be a limiting factor on the contour machining process since it is not accurate, forcing the machinist to work from an approximation of the true work-piece surface geometry rather than the real three-dimensional surface. Therefore, the resultant machined surface is not smooth and the file size is also enormous. As the tool path is defined by shorter line-segments, it will generate a more accurate definition of the part surface definition, but results in enormous amounts of data (Herrin 1995).

For machining of curved surfaces, a milling cutter suitably oriented to the surface normal is usually directed from point to point on a surface mesh with linearly interpolated motion. For many applications this can result in thousands of small linearly interpolated and repeated 'stop and go' moves across the surface. To solve these problems, Vickers (1992) developed a recursive curve-fitting algorithm. The approach is to fit a circular arc, within a prescribed error tolerance, through given specific surface data points. Unnecessary surface points are eliminated to produce a concise tool path program. Circular interpolation provides an excellent way to define a very accurate circle or circular segment with a very little amount of data.

Hu et al. (1998) proposed a layered shape rough machining technique to overcome the tool depth limitations. This means that an object that has a large depth or height will not be machined in just one pass, but will need a $2^{\text {nd }}$ or $3^{\text {rd }}$ machining layer. This strategy is needed for deep pocket machining because they are usually produced from a billet by 2.5 D roughing and $3 D$ and $5 D$ finishing.

Joo and Cho (1999) developed a feature-based technique for NC pocketing. Bulky pocket features were decomposed into compact features organized in several thin layers. The efficiency in machining the bulky feature is largely dependent on the cutter specification and cutting parameters. Consequently, the factors affecting machining efficiency should be considered in extracting pocket features.

Suh and Shin (1996) modeled pocket machining as a TSP (Traveling Salesman Problem) optimization problem. They used a neural network formulation to solve the optimization problem.

In summary, the tool path planning algorithms determine the tool path motion in an optimal fashion ensuring adequate coverage of the pocket. The surface roughness is minimized and a compact representation for the tool path is desired. Further, the machining time needs to be as small as possible.

## CHAPTER 3. POCKET DEFINITION AND NAVIGATION

### 3.1 Surface Definition

The bottom surface defined in this study is a Bezier surface. Bezier surface formulation uses a control net of points. Points on the Bezier surface are given by

$$
P(u, v)=\sum_{i=0}^{m} \sum_{j=0}^{n} B_{i, m}(u) B_{j, n}(v) P_{i j} \quad u, v \in[0,1]
$$

where $P_{i j}$ are the vertices of the control polygon and $B_{i, m}$ and $B_{j, n}$ are the Bernstein blending functions. In matrix form, we may describe the Bezier surface patch by the equation.

$$
\begin{aligned}
& P=P(u, v)=\left[\begin{array}{llll}
1 & u & u^{2} & u^{3}
\end{array}\right] M B M^{T}\left[\begin{array}{llll}
1 & v & v^{2} & v^{3}
\end{array}\right]^{T} \\
& M=\left[\begin{array}{rrrr}
1 & 0 & 0 & 0 \\
-3 & 3 & 0 & 0 \\
3-6 & 3 & 0 \\
-1 & 3-3 & 1
\end{array}\right] \quad, \quad B=\left[\begin{array}{llll}
p_{00} & p_{01} & p_{02} & p_{03} \\
p_{10} & p_{11} & p_{12} & p_{13} \\
p_{20} & p_{21} & p_{22} & p_{23} \\
p_{30} & p_{31} & p_{32} & p_{33}
\end{array}\right]
\end{aligned}
$$

The control points control the shape of the Bezier surface. Bezier surfaces pass through the corner control points and have edge curves that are tangential to the edges. They also have variation diminishing, and convex hull properties. Figure 3 shows a representative Bezier surface.


Figure 3. A Representative Bezier Surface

### 3.2 Grid Definition

The notion for grid based navigation stems from the guidance of autonomous guidance vehicles in unknown terrain and in the absence of vision feedback. First, the machined region is, assumed to be divided into a grid with size equal to or less than $D / \sqrt{2}$ where D is the diameter of the tool as shown in Figure 4. The reason for this is that when the centers of grid and tool are coincidental, the area covered by the tool should enclose the entire area of the grid. This would ensure that that no uncut material is left by the tool path. If the grid sizes are bigger than $D / \sqrt{2}$, there would be some uncut material at certain locations. From Figure 4, the following assumption can be made and then questioned.
"Whenever a cutter passes through the center point of each grid, this grid is completely removed because cutter will cover entire area of each grid."

This assumption will be true only when the pocket's bottom is planar. When the pocket has an arbitrarily shaped bottom surface, the cut portion is clean only in XY view (top view). Uncut material may remain in XZ and YZ views. This is because the tool did not pass through all adjacent grid points. This situation will occur, whenever there are any regions that the tool center does not pass through all 4 directions in X or Y .


Figure 4. Digitization of Bottom and Tool Path Motion in XY View

With Figure 5, a comprehensive explanation of the uncut material can be made. Regardless of tool path type, like window-frame or staircase, let's assume that the tool path goes through all points ( $\mathrm{A}, \mathrm{B}, \mathrm{C}, \mathrm{D}$, and E ) and bottom surface is sculptured surface. If there are direct motions only from grid $E$ to grid $D$ and from grid $E$ to grid $B$, there would be uncut material between grid E and grid A and between grid E and grid C . This contributes to the scallop height and it depends on tool diameter and grid size. The side view of the cutting situation is illustrated in Figure 6.

------------. : Enclosed area of tool at each grid
: Grid and tool center points at each location
: Grid

Figure 5. Possible Tool Moving Directions at Current Location


Tool Position B
a) Tool moves directly from $A$ to $B$


Tool Position B
b) Tool does not move directly from A to B

Figure 6. Side View Corresponding to the Tool Path

To solve this problem, the final NC tool path needs to be generated such that all uncut material is removed. Therefore, extraneous X zigzag and Y zigzag motions are needed for later execution to produce a smooth surface. However, these may be required only when better surface is necessary since more machining time is required for these additional operations.

### 3.3 Definition of Polygon

A general polygon can include both convex and concave shapes. A pocket with arbitrary wall geometry should therefore be a general polygon. Examples of convex and concave polygons are presented in Figure 7.

Vertex points are input to define a polygon. If the input polygon is rectangular or diagonal, it is required to input four vertices. As the polygon shape is more complex, it may

a) 3 Polygons having only convex shape

b) Polygon has both convex and concave shape

Figure 7. General Polygons with Convex and Concave Shape
require more number of vertices. Input vertex points (polygon points) are required to be at the intersection of the grids. It is to be noted that the tool center points should not be the same as grid center points because of problems with possible over-cutting for pocket boundary machining in XY view (see Figure 8).


Figure 8. An Example of a Defined Polygon

As can be seen from the Figure 8, the tool centers are not at the same locations as grid centers. If these are the same, it will cause over-cut. So the amount of gap should be calculated when wall (boundary) machining is being done to prevent over-cut.

### 3.4 Navigation Strategies

Before the details of the proposed methodology are given, two important aspects are discussed first: selection of mapping grid size and navigation strategies. The mapping grid size is selected as a function of the cutter diameter. As shown earlier in Figure 4, if the grid
size is taken as equal to $1 / \sqrt{2}$ of cutter diameter then the tool overlap between two consecutive and parallel grids will be equal to the difference between cutter diameter and mapped gird size. This amount of overlap is sufficient to clean away any residual material left between the two passes, especially when flat end milling tools are used for flat bottom surface.

The navigation strategy uses a priority such that the first permissible direction is in a counterclockwise sequence. After finding the nearest legitimate grid first, the tool moves there so that milling can go on until the pocket is completely traversed. The overall procedure showing detail information about navigation strategy can now be specified as shown in Figures 9, 10, 11, and 12. These figures show all possible directions of tool path from the current tool positions depending on the direction of previous position to current position.


Figure 9. Checking Navigation Condition When Precedent Navigation was $+X$ Direction

Priority 1: +Y
Priority 2: -X
Priority 3: -Y
Priority 4: +X
Each end point is tool center
SN means Successive Navigation


## Figure 10. Checking Navigation Condition When Precedent Navigation was -X Direction



Figure 11. Checking Navigation Condition When Precedent Navigation was $+\mathbf{Y}$ Direction

Priority 1:-X
Priority 2: -Y
Priority 3: +X
Priority 4: +Y
Each end point is tool center SN means Successive Navigation


## Figure 12. Checking Navigation Condition When Precedent Navigation was -Y Direction

P on each figure means precedent position. As P approaches to the current position, the direction is expressed as a dotted line. At each current position (at each center point of figures), there are 4 priorities. If there is no obstruction or no previous cut, the tool moves to the direction of priority 1 . If not it will be checked for priority 2 whether there is any obstruction or previous cut. If there is no obstruction for priority 2 , the tool will move to that direction. Priority 3 and 4 are tested in a similar fashion if there are obstructions for both priority 1 and 2 directions. X and Y zigzag motions are shown as dashed lines. These motions are made depending on the successive number that results in a priority number. Depending on the precedent navigation's direction, all 4 cases are shown. The following definitions are useful in defining the algorithm.

## Definitions

Precedent Navigation (P): Direction from previous to current point (each
center point of the figures)
Successive Navigation (SN): Direction from current point to next point
Priority Number: Direction that has a priority on precedent navigation

### 3.5 Pocket Machining Algorithm

Input values are: a. Vertex points of a polygon
b. Tool diameter
c. Grid size in X direction
d. Grid size in Y direction
a) Interior navigation for main tool path

1. Model the sculptured bottom Bezier surface with Z direction's control points.
2. Digitize the 2D shape in $X Y$ as a function of tool diameter and grid size in $X$ and $Y$ directions.
3. Depending on the number of digitized grids in XY plane, determine the unit parameter value ( $u$ and $v$ ) in X and Y directions from Bezier surface in step 1.
4. Match each $X$ and $Y$ value from step 2 with $Z$ values from step 3 based on an ordered specification. Call this set K. Finally all surface coordinates are determined in relation to the tool diameter, X and Y grid size.
5. Find a set of edge cutter extreme points (tool center point) at every vertex (polygon point) defined by user. Call this set $C$.
6. Make a new polygon based on C.
7. Determine the set of all grid centers inside the new polygon found in step 5. Call this new set S.
8. Find the navigation path from the point that has the left-most minimum $Y$ value by using proposed navigation procedure. Call this set U. And keep the path made by X zigzag and Y zigzag algorithm separately and find Z values by using set K . Call this set N (Zigzag motions).
9. Reverse the navigation path $(\mathrm{U})$ and find Z values by using set K . Call this set P (Main tool path)
b) Finding a path for wall machining, and combine with main, X zigzag, and Y zigzag tool paths.
10. Find the nearest neighborhood point within set C to begin wall machining.
11. Calculate tool centers between every two vertex in set C. Call this set $F$.
12. Sort the counterclockwise order of set $C$ and set $F$, then find $Z$ values by using set $K$. Call this new set $W$ (Pocket wall path).
13. Make a final navigation path such that $T=\{P \cup W \cup N\}$.
14. Determine the main tool path machining or simulation method among line movements, arc + line movements, and Bezier curve + line movements.

This NC pocketing algorithm can be summarized as shown in Figure 13. The polygon defined in the case study has the shape as shown in Figure 14 in XY view. Outer thick lines denote the pocket boundary. Inside the pocket boundary, there are thin lines connecting each cutter edge extreme point. Inner thick lines are the boundary of main tool path grids that are located inside of thin lines. Inside the inner thick line boundary, the tool path consists of the


Figure 13. Flowchart for NC Pocketing
main tool path, X zigzag, and Y zigzag machining. Wall machining is performed on the outside of inner thick lines.

Cutter edge extreme points Thick line is boundary of inside grids


Figure 14. Initial Preprocessing Procedure

## CHAPTER 4. MACHINING PATH AND NC CODE GENERATION

There are 3 methods used in this study for generating machining path categorized by tool movements. These are line movements, arc + line movements, and Bezier curve + line movements.

### 4.1 Line Movements

Line movements are done by linear interpolation. Linear moves can be made by one or any combination of all the active axes ( $\mathrm{X}, \mathrm{Y}, \mathrm{Z}$ ). An example is shown in Figure 15.

As it can be seen in Figure 15, there are consecutive linear motions to generate a mountain + valley shape curve. In this case, the advantage is that there is no need of changing active axis plane, just next destination coordinate ( $\mathrm{X}, \mathrm{Y}$, and Z ) needs to be specified after one movement. However, the disadvantages are that there are a lot of 'stop and go' motions that cause machining time delay and large file sizes.


Figure 15. Linear Movements to Generate Curve

### 4.2 Arc + Line Movements

The algorithm presented in this study is similar to that used by Vickers and Bradley (1992) which is a recursive approach to fit circular arcs, within a prescribed error tolerance, through surface data points. Unnecessary surface points are eliminated and linear interpolation segments are used only where necessary to produce a concise tool path program. The segmentation algorithm in case of XZ plane proceeds as follows.

1. Start with a set of cross-sectional points $\left(X_{i}, Z_{i}\right), i=1, \ldots, N$. If $N=2$, linear interpolation is formed.
2. Calculate the data set mid-point.
3. Calculate the arc center through the first, mid, and last points.
4. Calculate and test the error between the arc and the intermediate surface points. The error is given as

$$
\begin{aligned}
& \text { Error }=|r-d| \\
& \qquad\left|r-\left[\left(X_{i}-X_{c}\right)^{2}+\left(Z_{i}-Z_{c}\right)^{2}\right]^{1 / 2}\right|
\end{aligned}
$$

where $d$ is the distance to the data point $\left(X_{i}, Z_{i}\right)$ from the $\operatorname{arc}$ center $\left(X_{c}, Z_{c}\right)$ and $r$ is the arc radius.
5. If the test fails(exceeding the specified maximum error tolerance), the span of the arc is decreased from $\{i=1, \ldots, N\}$ to $\{i=1, \ldots, N-1\}$
6. If the test passes, the radius of the arc is checked to see if it is larger than specified (whether the radius goes to unlimited value). If so, a linear command is formed from start to end point.
7. If the radius of the arc is not larger than specified, the appropriate circular interpolation command is generated, otherwise $(\mathrm{N}=2)$ a linear interpolation command is generated.
8. The process is stopped if the last point is reached, otherwise a new arc center for the current location and the old end point is calculated.
9. The same algorithm is repeated for the next YZ plane and then it would finally stop at the end of the data point.

The decomposition of a curve into a set of lines and arcs is shown in Figure 16 and the entire algorithm is schematically shown in Figure 17. A circle of radius $r$ and center $(h, k)$ in XZ plane is expressed in implicit form to determine the center and radius of a circular arc passing through three data points. The form in YZ plane is the same as XZ plane.


Figure 16. Illustration of Arc + Line Movements


Figure 17. Flowchart of the Arc/Line Segmentation Algorithm in XZ Plane

$$
\begin{aligned}
& X^{2}+Z^{2}+a X+b Z+c=0 \\
& \text { where } a=-2 h, \quad b=-2 k \quad c=h^{2}+k^{2}-r^{2}
\end{aligned}
$$

A system of three equations, in the variables $a, b$, and $c$ are created for the data points $\left\{\left(\mathrm{X}_{1}, \mathrm{Z}_{1}\right),\left(\mathrm{X}_{2}, \mathrm{Z}_{2}\right),\left(\mathrm{X}_{3}, \mathrm{Z}_{3}\right)\right\}$, all of with lie on the arc. The matrix form of three equations is as follows.

$$
\left[\begin{array}{lll}
X_{1} & Z_{1} & 1 \\
X_{2} & Z_{2} & 1 \\
X_{3} & Z_{3} & 1_{\lrcorner} c
\end{array}\right]\left[\begin{array}{l}
a \\
b \\
-\left(X_{3}^{2}+Z_{3}^{2}\right)
\end{array}\right]=\left[\begin{array}{l}
-\left(X_{1}^{2}+Z_{1}^{2}\right) \\
-\left(X_{2}^{2}+Z_{2}^{2}\right) \\
-
\end{array}\right.
$$

### 4.3 Bezier Curve + Line Movements

With Bezier curve motion, more efficient tool path is generated. Bezier curve equations can be made using given surface points. First and last control points are start and end points. The problem is how to find $2^{\text {nd }}$ and $3^{\text {rd }}$ control points. With approximation skill, the problem has been solved.

The explicit form of cubic Bezier curve equation is as shown below.

$$
P(u)=P_{0}(1-u)^{3}+3 P_{1} u(1-u)^{2}+3 P_{2} u^{2}(1-u)+P_{3} u^{3} \quad 0 \leq u \leq 1
$$

$u_{1}$ and $u_{2}$ can be input to make two equations of two variables, which are

$$
\begin{aligned}
& u_{1}=\frac{1}{(n-1)}, \quad u_{2}=1-u_{1} \text { where } \mathrm{n} \text { is the number of points } \\
& P\left(u_{1}\right)=P_{0}\left(1-u_{1}\right)^{3}+3 P_{1} u_{1}\left(1-u_{1}\right)^{2}+3 P_{2} u_{1}^{2}\left(1-u_{1}\right)+P_{3} u_{1}^{3} \quad 0 \leq u_{1} \leq 1 \\
& P\left(u_{2}\right)=P_{0}\left(1-u_{2}\right)^{3}+3 P_{1} u_{2}\left(1-u_{2}\right)^{2}+3 P_{2} u_{2}^{2}\left(1-u_{2}\right)+P_{3} u_{2}^{3} \quad 0 \leq u_{2} \leq 1
\end{aligned}
$$

An assumption made in this approach is that the coordinates of $P\left(u_{1}\right)$ and $P\left(u_{2}\right)$ are equal to the $2^{\text {nd }}$ grid center point and $(n-1)^{\text {th }}$ grid center point when a Bezier curve is given $n$ surface points. This is shown in Figure 18.

A Bezier curve shown in Figure 19-(b) is expressed as a straight line. $P\left(u_{i}\right)$
$(i=1, \ldots, n)$ has exactly the same coordinates as grids in this case since the grids size are equal to $P\left(u_{i+1}\right)-P\left(u_{i}\right)$ which is a unit Bezier curve. However, as Bezier curve's curvature becomes larger, a unit Bezier curve size is bigger than a grid size (Figure 19-(a)). It causes surface point error in Z direction. As can be seen in Figure 19, those points' error will be larger as curvature of curve is larger. Surface point error can be approximated as follows as shown in Figure 20.


Figure 18. Generation of Bezier Curve Tool Path


Figure 19. Unit Distance in Bezier Curve


Figure 20. Surface Point Error in Bezier Curve
$\sqrt{(\text { Unit distance })^{2}+(Z \text { incremental })^{2}}: Z$ incremental

$$
\cong \sqrt{(\text { Unit distance })^{2}+(Z \text { incremental })^{2}}-\text { Unit length:Surface Point Error }
$$

Surface Point Error $\equiv \frac{\text { Zincremental }\left(\sqrt{(\text { Unit distance })^{2}+(Z \text { incremental })^{2}}-\text { Unit length }\right)}{\sqrt{(\text { Unit distance })^{2}+(Z \text { incremental })^{2}}}$

The algorithm is as follows.

1. Start with a set of cross-sectional points $\left(X_{i}, Z_{i}\right), i=1, \ldots, N$.
2. If $\mathrm{N}>3$, calculate $P\left(u_{1}\right)$ and $P\left(u_{2}\right)$ which correspond to the second ( $X_{2}$ ) point and ( n $1)^{\text {th }}\left(X_{n-1}\right)$ point. If not, linear interpolation is formed.
3. Calculate intermediate control points.
4. The same algorithm is repeated for the next YZ plane $\left[\left(Y_{i}, Z_{i}\right): \mathrm{i}=1, \ldots, \mathrm{~N}\right]$ and then it would finally stop at the end of the data point.

The algorithm generating Bezier curve + line movements is also shown in Figure 21.


Figure 21. Bezier Curve + Line Movements Algorithm in XZ Plane

### 4.4 Rough and Finish Cut

In most real machining situations, it is required to separate machining depth into some layers to protect tools from deflection and wear and to overcome the limitation of the tool length. These steps are necessary especially in deep pocket machining. Dividing machining into a number of layers means that there would be a different shape at each layer.

The proposed method in this study is controlling Z coordinates on the bottom surface points. This means that Z coordinates of surface points need to be specified to fit each layer's specification range. A simple 2D example is in Figure 22.


Figure 22. An Example of Rough Cutting Steps in 2 Dimensions

Since machining depth ( $Z$ coordinate) is concerned, this approach is selected for the main navigation tool path. From the top view, X and Y grid navigation of tool path is the same for each layer. After final layer's tool path machining followed by $1^{\text {st }}$ to $5^{\text {th }}$, pocket wall, X zigzag, and Y zigzag machining paths would be followed. If curvature at a certain layer is steep relative to other layers, the unit depth of that layer can be modified flexibly.

At each layer, there is a range of $Z$ values, such as $-0.1 \mathrm{in}<\mathrm{Z}<0$ (top surface), -0.2 in $<\mathrm{Z}<-0.1$ in, and -0.3 in $<\mathrm{Z}<-0.2$ in etc. If Z values of the bottom surface belong to each layer's $Z$ value zone at each layer machining time, those $Z$ values would be changed into the highest layer's Z value bigger than the maximum Z value of the bottom surface to prevent unwanted cut which includes over-cut.

Another advantage of this approach is controlling machining speed. For rough machining, quality is not an important factor. So it allows increasing machining speed for roughing, then final layer is machined with proper speed.

The final layer can be machined by 3 choices (line, arc + line, Bezier curve + line) introduced in previous sections.

### 4.5 Proposed Algorithm for Reverse Engineering

Since the bottom surface is defined with coordinates of (X,Y,Z), it can be applied to reverse engineering. For instance, there is an object that someone wants to machine and there is no existing CAD model. If the object can be reverse engineered or, in other words, those coordinates can be measured by devices like CMM (Coordinate Measurement Machine), then the surface can be machined using the pocketing algorithm described here regardless of the type of the surface. This is an advantage of the surface generation method used in this study. The reverse engineering procedure is shown in Figure 23.

Surface data is defined by coordinate points, depending upon the tool diameter in XY view. These data are then matched with $Z$ data points determined by control points. It means that as long as the measuring device traverses the data points with this unified grid method in XY view and measures the depth in Z direction, the surface would be generated with no


Figure 23. Proposed Reverse Engineering Algorithm


Figure 24. An Example of Bottom Surface for Reverse Engineering
problem. As grids' size is made smaller, more accurate surface would be made. However, it would take more time to machine.

A sample object that has a bottom surface as in Figure 24 is measured to show this algorithm with CMM. Each unit grid size in X and Y is 0.3 inch.

## CHAPTER 5. CASE STUDY

Two case studies have been made in this study. These are to show general polygon and to show rough and finish cut. The actual machining G\&M code for the case study is shown in the Appendix.

Different colors are used in these case studies. Main tool path is expressed with red color. Wall machining is shown with green color. Blue and dark green colors are used for X zigzag and Y zigzag each. Machining samples are illustrated to show how navigation strategies work for general polygon case with line movements.

To show arc + line and Bezier curve + line machining, red color of main machining is replaced by blue (thick) for arc and Bezier curve machining and yellow (light) for line movements. The algorithm for NC pocketing is implemented in Visual C++ and OpenGL.

1. Input
a. Vertex points of a polygon
b. Tool diameter: 0.25 in
c. Grid size in X direction: 0.125 in
d. Grid size in Y direction: 0.0625 in
2. Output
a. Output is a set of cutter paths to remove the inside area of a general polygon with an arbitrarily shaped bottom surface.
b. Drawing of the sculptured bottom surface with the defined polygon.

### 5.1 General Polygon

### 5.1.1 Line movements

The sequence of machining shown in this study is main tool path first (Figure 25), wall machining next (Figure 26). Then $X$ zigzag (Figure 27) and Y zigzag (Figure 28) machining are subsequently done. Finally, there is no left over area without direct movement between grid center points. In other words, all grids are connected to each other. Real .machining samples are shown in Figure 29 and the final simulation result is displayed in Figure 30.

### 5.1.2 Arc + line movements

Substituting linear main tool path to arc + line tool path is shown in Figure 31. Light (yellow) lines show linear movements between point to point and thick (blue) lines show arc movements for more than at least 3 points.

### 5.1.3 Bezier curve + line movements

These two figures for are + line movements and Bezier curve + line movements in Figure 31 and 32 show how these two methods are efficient in terms of saving a number of commands. With line movements only, all grid center points are connected by each unit line segments with red color. However, it shows clearly how these methods work. Of course, the total number of arc segments varies depending on the arc tolerance for arc + line movements. As tolerance is tighter, more arc segments or more line movements would be needed.

### 5.2 Rough and Finish Cut with Rectangle Pocket Shape

To avoid confusion due to many layers in the same shape of pocketing process, the total of 6 layers were divided into 2 figures (each 3 layers) as in Figure 33 and Figure 34. The
final layer is the main tool path. After final layer machining, pocket wall machining, X and Y zigzag machining is performed. The algorithms for these are the same as the previous case study.

### 5.3 Comments on Surface Error/Roughness/CL/CC

As shown in Figure 15, arc + line movements will have less surface error for a given tool path than line movements in terms of surface generation. In a given tolerance zone, arc + line algorithm generated arc tool path and line tool path was generated when necessary. Simply, arc movements would follow real surface points more accurately while line movements make an approximation. Surface roughness (Scallop height) is proportional to the relation between tool diameter and grid size as shown in Figure 35. As tool diameter become larger on a given grid size, surface roughness would be reduced. The case of arc + line movements would have smaller value of roughness because of the same reason as surface error.

The point that needs to be considered is the relation between CL (Cutter Location) and CC (Cutter Contact) of the tool. Tools move along the center points of the grids except for pocket wall machining. It means that tools go to and from center points (CL). If the bottom surface is smooth, CL and CC would be almost same. However, if the bottom surface is steep, tt would be different. The magnitude of the difference between CL and CC points is also proportional to tool diameter and grid size. So when complex and more accurate surface need to be designed, this point should be considered.


Figure 25. Isometric and Top Views of the Main Tool Path


Figure 26. Isometric and Top Views of the Pocket Wall Tool Path


Figure 27. Intermediate and Full Processing of X zigzag Tool Path


Figure 28. Intermediate and Full Processing of Y zigzag Tool Path


Figure 29. Real Machining Samples


Figure 30. Isometric and Top Views of Final Result after
Main, Wall, X and Y zigzag Tool Path


Figure 31. Arc + Line Movements on the Same Polygon


Figure 32. Bezier Curve + Line Movements on the Same Polygon


Figure 33. $\mathbf{1}^{\text {st }}, \mathbf{2}^{\text {nd }}$, and $3^{\text {rd }}$ layers of Rough \& Finish Cut


Figure 34. $4^{\text {th }}, 5^{\text {th }}$, and Final Layers of Rough \& Finish Cut

$\theta=\tan ^{-1}(Z$ incremental / unit grid size $)$
$R \cos \theta \cong R$-Surface Error
Surface Error $\cong R(1-\cos \theta)$

$$
\sqrt{\text { unit grid size }}+(R-\text { Zincremental })^{2}: R \cos \theta
$$

$$
\begin{aligned}
& \cong \sqrt{\text { unit grid size } e^{2}+\left(R-\text { Zincremental }^{2}\right.}-R: \text { Scallop Height } \\
& \text { Scallop Height } \cong \frac{R \cos \theta\left(\sqrt{\text { unit grid size } e^{2}+\left(R-\text { Zincremental }^{2}\right.}-R\right)}{\sqrt{\text { unit grid size } e^{2}+\left(R-\text { Zincremental }^{2}\right.}}
\end{aligned}
$$

Figure 35. Relation of CL, CC, and Surface Error

## CHAPTER 6. CONCLUSIONS

An algorithm to generate final NC codes for machining the general polygon with a sculptured bottom surface was presented. It is an improvement on the classical windowframe approach with an added component that the cutting direction is either in X or in Y axis making the cutting particularly simple to implement on a 3-axis CNC machine. The methodology can be applied to all convex and concave shaped polygons, and even though the polygon has more complicated bottom surfaces, this algorithm works.

A grid based navigation strategy is used in planning the tool motion. The cutter path consists of the interior main tool path, machining along the periphery (wall machining), and X and Y zigzag motion. The X and Y zigzag motion commands are added to reduce the surface roughness. The wall machining is performed to improve the surface finish and accuracy along the walls of the pocket. A unified rough and finish cut algorithm is incorporated to machine deep pockets. This is necessary because the machining depth is limited by the length and rigidity of the cutting tool.

The grid based navigation strategy lays a foundation for the implementation of curvilinear interpolation algorithms. Three strategies, namely, line, arc + line, and Bezier curve + line movements were implemented for NC tool path generation in this study. All the methods were graphically simulated. The graphical simulations show that arc + line and Bezier curve +line methods can remove the excessive data points, and thus reduce the size of NC program compared to line movement. And we know by appeal to analytical proof that this algorithm should improve the smoothness of the final bottom surface and machining time since it has less data points and greatly reduced 'stop and go' motions. The amount of
saved data files and machining time will vary depending on how the pocket polygon is defined.

The navigation algorithm was experimentally validated for linear machining on a 3 axis CNC machine. Experimental verification of curvilinear interpolation techniques are part of planned future research work. We expect these experimental results to match with those predicted by the simulations. Future work also is planned in the development of generalpurpose curvilinear interpolation controllers for CNC machine tools. There has been significant work in the development of open architecture controllers to serve this purpose, however they are still not "open" enough and we expect to further work on the hardware control infrastructure to support the implementation of general purpose curvilinear interpolation algorithms.

## APPENDIX

# Generated G\&M Codes for General Polygon Case with Line Movements 

/* Start main tool path machining */

N0G5M3
N1G90G0Z0.5F3
N2X1.275000Y1.212500G01
N3Z-0. 295210
N4X1.150000Y1.212500Z-0.289395 N5X1.025000Y1.212500Z-0.284524 N6X1.025000Y1.275000Z-0.286268 N7X1.150000Y1.275000Z-0.291204 N8X1.275000Y1.275000Z-0.297095 N9X1.400000Y1.275000Z-0.303464 N10X1. 525000Y1.275000Z-0.309833 N11X1.650000Y1.275000Z-0.315724 N12X1.775000Y1.275000Z-0.320661 N13X1.775000Y1.212500Z-0.318469 N14X1. $650000 \mathrm{Y} 1.212500 \mathrm{Z}-0.313597$ N15X1.525000Y1.212500Z-0.307782 N16X1.400000Y1.212500Z-0.301496 N17X1.400000Y1.150000Z-0.301496 N18X1. $275000 \mathrm{Y} 1.150000 \mathrm{Z}-0.295210$ N19X1.150000Y1.150000Z-0.289395 N20X1.025000Y1.150000Z-0.284524 N21X0.900000Y1.150000Z-0.281066 N22X0.900000Y1.212500Z-0.281066 N23X0.900000Y1.275000Z-0.282765 N24X0.900000Y1.337500Z-0.286161 N25X1.025000Y1.337500Z-0.289756 N26X1. 150000Y1. $337500 \mathrm{Z}-0.294820$ N27X1. $275000 \mathrm{Y} 1.337500 \mathrm{Z}-0.300865$ N28X1.400000Y1.337500Z-0.307400 N29X1. 525000Y1.337500Z-0.313935 N30X1. $650000 \mathrm{Y} 1.337500 \mathrm{Z}-0.319980$ N31X1. $775000 \mathrm{Y} 1.337500 \mathrm{Z}-0.325045$ N32X1.900000Y1.337500Z-0.328639 N33X1.900000Y1.275000Z-0.324164 N34X1.900000Y1. $212500 \mathrm{Z}-0.321926$ N35X1.900000Y1. 150000Z-0.321926 N36X1.775000Y1.150000Z-0.318468 N37X1.650000Y1.150000Z-0.313597 N38X1.525000Y1.150000Z-0.307782 N39X1. 525000Y1.087500Z-0.309833 N40X1.400000Y1.087500Z-0.303464 N41X1.275000Y1.087500Z-0.297095 N42X1. 150000Y1.087500Z-0.291204 N43X1.025000Y1.087500Z-0.286268 N44X0.900000Y1.087500Z-0.282765 N45X0.775000Y1.087500Z-0.281172 N46X0.775000Y1.150000Z-0.279495

N47X0.775000Y1.212500Z-0.279495 N48X0.775000Y1.275000Z-0.281172 N49X0.775000Y1.337500Z-0.284528 N50X0.775000Y1.400000Z-0.289560 N51X0.900000Y1.400000Z-0.291256 N52X1.025000Y1. $400000 \mathrm{Z}-0.294988$ N53X1. 150000Y1. 400000Z-0.300245 N54X1.275000Y1. $400000 \mathrm{Z}-0.306520$ N55X1.400000Y1.400000Z-0.313304 N56X1.525000Y1.400000Z-0.320088 N57X1.650000Y1.400000Z-0.326363 N58X1.775000Y1.400000Z-0.331621 N59X1.900000Y1.400000Z-0.335352 N60X2.025000Y1.400000Z-0.337048 N61X2.025000Y1.337500Z-0.330273 N62X2.025000Y1.275000Z-0.325756 N63X2.025000Y1.212500Z-0.323497 N64X2.025000Y1.150000Z-0.323497 N65X2.025000Y1.087500Z-0.325756 N66X1.900000Y1.087500Z-0.324164 N67X1.775000Y1.087500Z-0.320661 N68X1.650000Y1.087500Z-0.315724 N69X1.650000Y1.025000Z-0.319980 N70X1. $525000 \mathrm{Y} 1.025000 \mathrm{Z}-0.313935$ N71X1.400000Y1.025000Z-0.307400 N72X1.275000Y1.025000Z-0.300865 N73X1.150000Y1.025000Z-0.294820 N74X1.025000Y1.025000Z-0.289756 N75X0.900000Y1.025000Z-0.286161 N76X0.775000Y1.025000Z-0.284528 N77X0.650000Y1.025000Z-0.285344 N78X0.650000Y1.087500Z-0.281968 N79X0.650000Y1. $150000 \mathrm{Z}-0.280280$ N80X0.650000Y1. $212500 \mathrm{Z}-0.280280$ N81X0.650000Y1.275000Z-0.281968 N82X0.650000Y1.337500Z-0.285344 N83X0.650000Y1.400000Z-0.290408 N84X0.650000Y1.462500Z-0.297160 N85X0.775000Y1.462500Z-0.296271 N86X0.900000Y1.462500Z-0.298050 N87X1.025000Y1.462500Z-0.301964 N88X1.150000Y1.462500Z-0.307478 N89X1.275000Y1.462500Z-0.314060 N90X1. $275000 \mathrm{Y} 1.525000 \mathrm{Z}-0.323486$ N91X1.400000Y1.525000Z-0.331016 N92X1.400000Y1.462500Z-0.321176 N93X1.525000Y1.462500Z-0.328292

N94X1.650000Y1.462500Z-0.334874 N95X1.775000Y1.462500Z-0.340389 N96X1.900000Y1.462500Z-0.344302 N97X2.025000Y1.462500Z-0.346081 N98X2.150000Y1.462500Z-0.345192 N99X2.150000Y1.400000Z-0.336200 N100X2.150000Y1.337500Z-0.329456 N101X2.150000Y1.275000Z-0.324960 N102X2.150000Y1.212500Z-0.322712 N103X2.150000Y1.150000Z-0.322712 N104X2.150000Y1.087500Z-0.324960 N105X2.150000Y1.025000Z-0.329456 N106X2.025000Y1.025000Z-0.330272 N107X1. $900000 \mathrm{Y} 1.025000 \mathrm{Z}-0.328639$ N108X1.775000Y1.025000Z-0.325044 N109X1.775000Y0.962500Z-0.331620 N110X1.775000Y0.900000Z-0.340388 N111X1.775000Y0.837500Z-0.351348 N112X1.775000Y0.775000Z-0.364500 N113X1.775000Y0.712500Z-0.379844 N114X1.775000Y0.650000Z-0.397380 N115X1.775000Y0.587500Z-0.417108 N116X1.650000Y0.587500Z-0.409343 N117X1.650000Y0.650000Z-0.390194 N118X1.650000Y0.712500Z-0.373172 N119X1.650000Y0.775000Z-0.358279 N120X1.650000Y0.837500Z-0.345512 N121X1.650000Y0.900000Z-0.334874 N122X1. $650000 \mathrm{Y} 0.962500 \mathrm{Z}-0.326363$ N123X1. $525000 \mathrm{Y} 0.962500 \mathrm{Z}-0.320088$ N124X1.400000Y0.962500Z-0.313304 N125X1.275000Y0.962500Z-0.306520 N126X1.150000Y0.962500Z-0.300245 N127X1.025000Y0.962500Z-0.294988 N128X0.900000Y0.962500Z-0.291256 N129X0.775000Y0.962500Z-0.289560 N130X0.650000Y0.962500Z-0.290408 N131X0. $525000 \mathrm{Y} 0.962500 \mathrm{Z}-0.294309$ N132X0. $525000 \mathrm{Y} 1.025000 \mathrm{Z}-0.289102$ N133X0.525000Y1.087500Z-0.285631 N134X0.525000Y1.150000Z-0.283895 N135X0.525000Y1.212500Z-0.283895 N136X0.525000Y1.275000Z-0.285631 N137X0.525000Y1.337500Z-0.289102 N138X0. 525000Y1.400000Z-0.294309 N139X0.525000Y1.462500Z-0.301252 N140X0.525000Y1.525000Z-0.309931 N141X0.650000Y1.525000Z-0.305600 N142X0.775000Y1.525000Z-0.304659 N143X0. $900000 \mathrm{Y} 1.5250002-0.306542$ N144X1.025000Y1.525000Z-0.310684 N145X1.150000Y1.525000Z-0.316520 N146X1.150000Y1.587500Z-0.327370 N147X1.275000Y1.587500Z-0.334796 N148X1.275000Y1.650000Z-0.347991

N149X1.400000Y1.650000Z-0.356600 N150X1.400000Y1.587500Z-0.342824 N151X1.525000Y1.587500Z-0.350852 N152X1.525000Y1.525000Z-0.338547 N153X1.650000Y1.525000Z-0.345512 N154X1.775000Y1.525000Z-0.351349 N155X1.900000Y1.525000Z-0.355490 N156X2.025000Y1. $525000 \mathrm{Z}-0.357373$ N157X2.150000Y1.525000Z-0.356432 N158X2.275000Y1.525000Z-0.352102 N159X2.275000Y1.462500Z-0.341100 N160X2.275000Y1.400000Z-0.332299 N161X2.275000Y1.337500Z-0.325698 N162X2.275000Y1. 275000Z-0.321297 N163X2.275000Y1.212500Z-0.319097 N164X2.275000Y1.150000Z-0.319097 N165X2.275000Y1.087500Z-0.321297 N166X2.275000Y1.025000Z-0.325698 N167X2.275000Y0.962500Z-0.332299 N168X2.150000Y0.962500Z-0.336200 N169X2.025000Y0.962500Z-0.337048 N170X1.900000Y0.962500Z-0.335352 N171X1.900000Y0.900000Z-0.344302 N172X1.900000Y0.837500Z-0.355490 N173X1.900000Y0.775000Z-0.368916 N174X1.900000Y0.712500Z-0.384580 N175X1.900000Y0.650000Z-0.402481 N176X1. $900000 \mathrm{Y} 0.587500 \mathrm{Z}-0.422619$ N177X1.900000Y0.525000Z-0.444996 N178X1.775000Y0.525000Z-0.439028 N179X1.650000Y0.525000Z-0.430620 N180X1. $525000 \mathrm{Y} 0.525000 \mathrm{Z}-0.420585$ N181X1.525000Y0.587500Z-0.400075 N182X1.525000Y0.650000Z-0.381617 N183X1.525000Y0.712500Z-0.365209 N184X1. $525000 \mathrm{Y} 0.775000 \mathrm{Z}-0.350852$ N185X1.525000Y0.837500Z-0.338547 N186X1. $525000 \mathrm{Y} 0.900000 \mathrm{Z}-0.328292$ N187X1.400000Y0. $900000 \mathrm{Z}-0.321176$ N188X1.275000Y0.900000Z-0.314060 N189X1.150000Y0.900000Z-0.307478 N190X1.025000Y0.900000Z-0.301964 N191X0.900000Y0.900000Z-0.298050 N192X0.775000Y0.900000Z-0.296271 N193X0.650000Y0.900000Z-0.297160 N194X0.525000Y0.900000Z-0.301252 N195X0.400000Y0.900000Z-0.309079 N196X0.400000Y0.962500Z-0.301771 N197X0.400000Y1.025000Z-0.296291 N198X0.400000Y1.087500Z-0.292637 N199X0.400000Y1.150000Z-0.290810 N200X0.400000Y1.212500Z-0.290810 N201X0.400000Y1.275000Z-0.292637 N202X0.400000Y1.337500Z-0.296291 N203X0.400000Y1.400000Z-0.301771

N204X0.400000Y1.462500Z-0.309079 N205X0.400000Y1. 525000Z-0.318214 N206X0.400000Y1. $587500 \mathrm{Z}-0.329176$ N207X0. 525000Y1. $587500 \mathrm{Z}-0.320345$ N208X0.650000Y1. $587500 \mathrm{Z}-0.315728$ N209X0.775000Y1.587500Z-0.314725 N210X0.900000Y1.587500Z-0.316732 N211X1.025000Y1.587500Z-0.321148 N212X1.025000Y1. $650000 \mathrm{Z}-0.333356$ N213X1.150000Y1.650000Z-0.340028 N214X1.150000Y1.712500Z-0.354494 N215X1.275000Y1.712500Z-0.363071 N216X1.275000Y1.775000Z-0.380037 N217X1.400000Y1. $775000 \mathrm{Z}-0.390056$ N218X1.400000Y1.712500Z-0.372344 N219X1.525000Y1.712500Z-0.381617 N220X1.525000Y1.650000Z-0.365209 N221X1. 650000Y1.650000Z-0.373173 N222X1.650000Y1.587500Z-0.358279 N223X1. $775000 \mathrm{Y} 1.587500 \mathrm{Z}-0.364501$ N224X1.900000Y1.587500Z-0.368916 N225X2.025000Y1.587500Z-0.370923 N226X2.150000Y1.587500Z-0.369920 N227X2.275000Y1.587500Z-0.365303 N228X2.400000Y1.587500Z-0.356472 N229X2.400000Y1.525000Z-0.343818 $\mathrm{N} 230 \mathrm{X} 2.400000 \mathrm{Y} 1.462500 \mathrm{Z}-0.333273$ N231X2.400000Y1.400000Z-0.324837 $\mathrm{N} 232 \mathrm{X} 2.400000 \mathrm{Y} 1.337500 \mathrm{Z}-0.318510$ N233X2.400000Y1.275000Z-0.314292 N234X2.400000Y1.212500Z-0.312182 N235X2.400000Y1. 150000Z-0.312182 N236X2.400000Y1.087500Z-0.314292 N237X2.400000Y1.025000Z-0.318510 N238X2.400000Y0.962500Z-0.324837 N239X2.400000Y0.900000Z-0.333273 $\mathrm{N} 240 \mathrm{X} 2.275000 \mathrm{Y} 0.900000 \mathrm{Z}-0.341100$ N241X2.150000Y0.900000Z-0.345192 N242X2.025000Y0. $900000 \mathrm{Z}-0.346081$ N243X2.025000Y0.837500Z-0. 357373 $\mathrm{N} 244 \mathrm{X} 2.025000 \mathrm{Y} 0.775000 \mathrm{Z}-0.370923$ N245X2.025000Y0.712500Z-0.386732 N246X2.025000Y0.650000Z-0.404799 N247X2.025000Y0.587500Z-0.425124 N248X2.025000Y0.525000Z-0.447708 $\mathrm{N} 249 \mathrm{X} 2.025000 \mathrm{Y} 0.462500 \mathrm{Z}-0.472550$ $\mathrm{N} 250 \mathrm{X1} .900000 \mathrm{Y} 0.462500 \mathrm{Z}-0.469609$ N251X1.775000Y0.462500Z-0.463140 N252X1.650000Y0.462500Z-0.454025 N253X1.525000Y0.462500Z-0.443146 /* Start wall machining */ N254G0Z0. 3 N255G1X1.501405Y0.434972F2 $\mathrm{N} 256 \mathrm{GOZ}-0.443146$ N257X1.626405Y0.434972Z-0.454025

N258X1.751405Y0.434972Z-0.463140 N259X1.876405Y0.434972Z-0.469609 N260X2.048596Y0.434972Z-0.471080 N261X2.048596Y0.497472Z-0.446352 N262X2.048596Y0.559972Z-0.423872 N263X2.048596Y0.622472Z-0.403640 N264X2.048596Y0.684972Z-0.385656 N265X2.048596Y0.747472Z-0.369920 N266X2.048596Y0.809972Z-0.356432 N267X2.048596Y0.872472Z-0.345192 N268X2.173596Y0.872472Z-0.341100 N269X2.298596Y0.872472Z-0.333273 N270X2.423596Y0.872472Z-0.321176 N271X2.423596Y0.934972Z-0.313304 N272X2.423596Y0.997472Z-0.307400 N273X2.423596Y1.059972Z-0.303464 N274X2.423596Y1.122472Z-0.301496 N275X2.423596Y1.184972Z-0.301496 N276X2.423596Y1.247472Z-0.303464 N277X2.423596Y1.309972Z-0.307400 N278X2.423596Y1.372472Z-0.313304 N279X2.423596Y1.434972Z-0.321176 N280X2.423596Y1.497472Z-0.331016 N281X2.423596Y1.615028Z-0.342824 N282X2.298596Y1.615028Z-0.356472 N283X2.173596Y1.615028Z-0.365303 N284X2.048596Y1.615028Z-0.369920 N285X1.923596Y1.615028Z-0.370923 N286X1.732296Y1.615028Z-0.364501 N287X1.607296Y1.688267Z-0.390194 N288X1.482296Y1.761506Z-0.400075 N289X1.337500Y1.846344Z-0.409736 N290X1.212500Y1.773105Z-0.380037 N291X1.087500Y1.699866Z-0.354494 N292X0.942704Y1.615028Z-0.321148 N293X0.817704Y1.615028Z-0.316732 N294X0.692704Y1.615028Z-0.314725 N295X0.567704Y1.615028Z-0.315728 N296X0.376404Y1.615028Z-0.329176 N297X0.376404Y1.552528Z-0.318214 N298X0.376404Y1.490028Z-0.309079 N299X0.376404Y1.427528Z-0.301771 N300X0.376404Y1.365028Z-0. 296291 N301X0.376404Y1.302528Z-0. 292637 N302X0.376404Y1.240028Z-0.290810 N303X0.376404Y1.177528Z-0.290810 N304X0.376404Y1.115028Z-0.292637 N305X0.376404Y1.052528Z-0.296291 N306X0.376404Y0.990028Z-0.301771 N307X0.376404Y0.872472Z-0.309079 N308X0. $501404 \mathrm{Y} 0.872472 \mathrm{Z}-0.301252$ N309X0.626404Y0.872472Z-0. 297160 N310X0.751404Y0.872472Z-0.296271 N311X0.876404Y0.872472Z-0.298050 N312X1.001404Y0.872472Z-0.301964

N313X1.126404Y0.872472Z-0.307478 N314X1.251404Y0.872472Z-0.314060 N315X1.376404Y0.872472Z-0.321176 N316X1. 501405Y0.872472Z-0.328292 N317X1.501405Y0.809972Z-0.338547 N318X1. 501405Y0.747472Z-0.350852 N319X1.501405Y0.684972Z-0.365209 N320X1. 501405Y0.622472Z-0.381617 N321X1.501405Y0.559972Z-0.400075 N322X1.501405Y0.497472Z-0.420585 N323X1.501405Y0.434972Z-0.443146
/* Start Y zigzag machining */ N324G0Z-0.1
N325G1X1.525000Y0.462500Z-0.1
N326G0Z-0.443146
N327G1X1.525000Y0.525000Z-0.420585 N328G0Z-0.1
N329G1X1.650000Y0.462500Z-0.1
N330G0Z-0.454025
N331G1X1.650000Y0.5250002-0.430620
N332G0Z-0.1
N333G1X1.775000Y0.462500Z-0.1
N334G0Z-0.463140
N335G1X1.775000Y0.525000Z-0.439028 N336G0Z-0.1
N337G1X1.900000Y0.462500Z-0.1
N338G02-0.469609
N339G1X1.900000Y0.525000Z-0.444996
N340G0Z-0.1
N341G1X2.025000Y0.900000Z-0.1
N342G0Z-0.346081
N343G1X2.025000Y0.962500Z-0.337048
N344G0Z-0.1
N345G1X2.150000Y0.900000Z-0.1
N346G0Z-0.345192
N347G1X2.150000Y0.962500Z-0.336200
N348GOZ-0.1
N349G1X2.275000Y0.900000Z-0.1
N350G0Z-0.341100
N351G1X2.275000Y0.962500Z-0.332299
N352G0Z-0.1
N353G1X2.275000Y1.587500Z-0.1
N354G0Z-0.365303
N355G1X2.275000Y1. $525000 \mathrm{Z}-0.352102$
N356G0Z-0.1
N357G1X2.150000Y1.587500Z-0.1
N358G0Z-0.369920
N359G1X2.150000Y1.525000Z-0.356432 N360G0Z-0.1
N361G1X2.025000Y1.587500Z-0.1
N362G0Z-0.370923
N363G1X2.025000Y1.525000Z-0.357373 N364G0Z-0.1
N365G1X1. $900000 \mathrm{Y} 1.587500 \mathrm{Z}-0.1$

N366G02-0.368916
N367G1X1.900000Y1.525000Z-0.355490 N368G0Z-0.1
N369G1X1.775000Y1.587500Z-0.1
N370G0Z-0.364501
N371G1X1.775000Y1.525000Z-0.351349 N372G0Z-0.1
N373G1X1.650000Y1.587500Z-0.1
N374G0Z-0.358279
N375G1X1.650000Y1.525000Z-0.345512
N376G0Z-0.1
N377G1X1.525000Y1.650000Z-0.1
N378G0Z-0.365209
N379G1X1.525000Y1.587500Z-0.350852
N380G0Z-0.1
N381G1X1.400000Y1.712500Z-0.1
N382G0Z-0.372344
N383G1X1.400000Y1.650000Z-0.356600
N384G0Z-0.1
N385G1X1.275000Y1.775000Z-0.1
N386G0Z-0.380037
N387G1X1.275000Y1.712500Z-0.363071
N388G0Z-0.1
N389G1X1.275000Y1.712500Z-0.1
N390G0Z-0.363071
N391G1X1.275000Y1.650000Z-0.347991
N392GOZ-0.1
N393G1X1.150000Y1.712500Z-0.1
N394G0Z-0.354494
N395G1X1. 150000Y1.650000Z-0.340028
N396G0Z-0. 1
N397G1X1.150000Y1.650000Z-0.1
N398G0Z-0.340028
N399G1X1.150000Y1.587500Z-0.327370
N400G0Z-0.1
N401G1X1.025000Y1.650000Z-0.1
N402G0Z-0. 333356
N403G1X1.025000Y1.587500Z-0.321148
N404G0Z-0. 1
N405G1X1.025000Y1.587500Z-0.1
N406G0Z-0.321148
N407G1X1.025000Y1.525000Z-0.310684
N408G0Z-0.1
N409G1X0.900000Y1.587500Z-0.1
N410G0Z-0.316732
N411G1X0.900000Y1.525000Z-0.306542
N412G0Z-0.1
N413G1X0.775000Y1.587500Z-0.1
N414G0Z-0.314725
N415G1X0.775000Y1.525000Z-0.304659
N416GOZ-0.1
N417G1X0.650000Y1.587500Z-0.1
N418G0Z-0.315728
N419G1X0.650000Y1.525000Z-0.305600 N420G0Z-0.1

N421G1X0.525000Y1.587500Z-0.1
N422GOZ-0. 320345
N423G1X0.525000Y1.525000Z-0.309931
N424G0Z-0.1
N425G1X0.400000Y1.587500Z-0.1
N426GOZ-0. 329176
N427G1X0.400000Y1.525000Z-0.318214 N428GOZ-0.1
N429G1X0.400000Y0.900000Z-0.1
N430G0Z-0. 309079
N431G1X0.400000Y0.962500Z-0.301771
N432G0Z-0.1
N433G1X0.525000Y0.900000Z-0.1
N434G0Z-0. 301252
N435G1X0.525000Y0.962500Z-0.294309
N436GOZ-0.1
N437G1X0.650000Y0.900000Z-0.1
N438G0Z-0. 297160
N439G1X0.650000Y0.962500Z-0.290408
N440G0Z-0.1
N441G1X0.775000Y0.900000Z-0.1
N442GOZ-0.296271
N443G1X0.775000Y0.962500Z-0. 289560
N444GOZ-0.1
N445G1X0.900000Y0.900000Z-0.1
N446GOZ-0.298050
N447G1X0.900000Y0.962500Z-0.291256
N448G0Z-0.1
N449G1X1.025000Y0.900000Z-0.1
N450GOZ-0. 301964
N451G1X1.025000Y0.962500Z-0.294988 N452G0Z-0.1
N453G1X1.150000Y0.900000Z-0.1
N454G0Z-0. 307478
N455G1X1.150000Y0.962500Z-0.300245 N456G0Z-0.1
N457G1X1.275000Y0.900000Z-0.1
N458GOZ-0.314060
N459G1X1.275000Y0.962500Z-0.306520 N460G0Z-0.1
N461G1X1.400000Y0.900000Z-0.1
N462G0Z-0.321176
N463G1X1.400000Y0.962500Z-0.313304 N464G0Z-0.1
N465G1X1.525000Y0.900000Z-0.1
N466G0Z-0.328292
N467G1X1.525000Y0.962500Z-0.320088 N468GOZ-0.1
N469G1X1.525000Y0.525000Z-0.1
N470G0Z-0.420585
N471G1X1.525000Y0.587500Z-0.400075
N472G0Z-0.1
N473G1X1.650000Y0.525000Z-0.1
N474GOZ-0.430620
N475G1X1.650000Y0.587500Z-0.409343
N476G0Z-0.1
N477G1X1.775000Y0.525000Z-0.1
N478G0Z-0.439028
N479G1X1.775000Y0.587500Z-0.417108
N480GOZ-0.1
N481G1X1.900000Y0.962500Z-0.1
N482G0Z-0.335352
N483G1X1.900000Y1.025000Z-0.328639
N484G0Z-0.1
N485G1X2.025000Y0.962500Z-0.1
N486G0Z-0. 337048
N487G1X2.025000Y1.025000Z-0.330272
N488G0Z-0.1
N489G1X2.150000Y0.962500Z-0.1
N490G0Z-0.336200
N491G1X2.150000Y1.025000Z-0.329456
N492G0Z-0.1
N493G1X2.150000Y1.525000Z-0.1
N494GOZ-0. 356432
N495G1X2.150000Y1.462500Z-0.345192
N496G0Z-0.1
N497G1X2.025000Y1.525000Z-0.1
N498G0Z-0. 357373
N499G1X2.025000Y1.462500Z-0.346081
N500GOZ-0.1
N501G1X1.900000Y1.525000Z-0.1
N502GOZ-0. 355490
N503G1X1.900000Y1.462500Z-0.344302
N504G0Z-0.1
N505G1X1.775000Y1.525000Z-0.1
N506G0Z-0.351349
N507G1X1.775000Y1.462500Z-0.340389
N508G0Z-0.1
N509G1X1.650000Y1.525000Z-0.1
N510G0Z-0.345512
N511G1X1.650000Y1.462500Z-0.334874
N512G0Z-0.1
N513G1X1.525000Y1.525000Z-0.1
N514G0Z-0. 338547
N515G1X1.525000Y1.462500Z-0.328292
N516GOZ-0.1
N517G1X1.400000Y1.587500Z-0.1
N518GOZ-0. 342824
N519G1X1.400000Y1.525000Z-0.331016
N520GOZ-0.1
N521G1X1.275000Y1.650000Z-0.1
N522G0Z-0.347991
N523G1X1.275000Y1.587500Z-0.334796
N524G0Z-0.1
N525G1X1.275000Y1.587500Z-0.1
N526G0Z-0. 334796
N527G1X1.275000Y1.525000Z-0.323486 N528G0Z-0.1
N529G1X1.150000Y1.587500Z-0.1
N530GOZ-0. 327370

N531G1X1.150000Y1.525000Z-0.316520
N532G0Z-0.1
N533G1X1.150000Y1.525000Z-0.1
$\mathrm{N} 534 \mathrm{GOZ}-0.316520$
N535G1X1.150000Y1.462500Z-0.307478
N536G0Z-0.1
N537G1X1.025000Y1.525000Z-0.1
N538G0Z-0.310684
N539G1X1.025000Y1.462500Z-0.301964 N540G0Z-0.1
N541G1X0.900000Y1.525000Z-0.1
N542G0Z-0. 306542
N543G1X0.900000Y1.462500Z-0.298050 N544G0Z-0.1
N545G1X0.775000Y1.525000Z-0.1
N546G0Z-0.304659
N547G1X0.775000Y1.462500Z-0.296271 N548G0Z-0.1
N549G1X0.650000Y1.525000Z-0.1
N550G0Z-0. 305600
N551G1X0.650000Y1.462500Z-0.297160
N552G0Z-0. 1
N553G1X0.525000Y1.525000Z-0.1
N554G0Z-0.309931
N555G1X0.525000Y1.462500Z-0.301252 N556G0Z-0.1
N557G1X0.525000Y0.962500Z-0.1
N558G0Z-0.294309
N559G1X0.525000Y1.025000Z-0.289102 N560G0Z-0.1
N561G1X0.650000Y0.962500Z-0.1
N562G0Z-0.290408
N563G1X0.650000Y1.025000Z-0.285344 N564G0Z-0.1
N565G1X0.775000Y0.962500Z-0.1
N566G0Z-0.289560
N567G1X0.775000Y1.025000Z-0.284528
N568G0Z-0.1
N569G1X0.900000Y0.962500Z-0.1
N570G0Z-0. 291256
N571G1X0.900000Y1.025000Z-0.286161
N572G0Z-0.1
N573G1X1.025000Y0.962500Z-0.1
N574G0Z-0.294988
N575G1X1.025000Y1.025000Z-0.289756
N576G0Z-0.1
N577G1X1.150000Y0.962500Z-0.1
N578G0Z-0. 300245
N579G1X1.150000Y1.025000Z-0.294820 N580G0Z-0.1
N581G1XI.275000Y0.962500Z-0.1
N582G0Z-0.306520
N583G1X1.275000Y1.025000Z-0. 300865 N584G0Z-0.1
N585G1X1.400000Y0.962500Z-0.1

N586G0Z-0. 313304
N587G1X1.400000Y1.025000Z-0.307400 N588G0Z-0.1
N5 89G1X1.525000Y0.962500Z-0.1
N590G0Z-0.320088
N591G1X1.525000Y1.025000Z-0.313935
N592G0Z-0.1
N593G1X1.650000Y0.962500Z-0.1
N594G0Z-0. 326363
N595G1X1.650000Y1.025000Z-0.319980
N596G0Z-0.1
N597G1X1.650000Y0.587500Z-0.1
N598GOZ-0.409343
N599G1X1.650000Y0.650000Z-0.390194 N600G0Z-0.1
N601G1X1.775000Y1.025000Z-0.1
N602G0Z-0.325044
N603G1X1.775000Y1.087500Z-0.320661
N604G0Z-0.1
N605G1X1.900000Y1.025000Z-0.1
N606G0Z-0.328639
N607G1X1.900000Y1.087500Z-0.324164
N608G0Z-0.1
N609G1X2.025000Y1.025000Z-0.1
N610G0Z-0.330272
N611G1X2.025000Y1.087500Z-0.325756
N612G0Z-0.1
N613G1X2.025000Y1.462500Z-0.1
N614G0Z-0. 346081
N615G1X2.025000Y1.400000Z-0.337048
N616G0Z-0.1
N617G1X1.900000Y1.462500Z-0.1
N618G0Z-0.344302
N619G1X1.900000Y1.400000Z-0.335352
N620G0Z-0.1
N621G1X1.775000Y1.462500Z-0.1
N622G0Z-0.340389
N623G1X1.775000Y1.400000Z-0.331621
N624G0Z-0.1
N625G1X1.650000Y1.462500Z-0.1
N626G0Z-0.334874
N627G1X1.650000Y1.400000Z-0.326363
N628G0Z-0.1
N629G1X1.525000Y1.462500Z-0.1
N630G0Z-0.328292
N631G1X1. $525000 \mathrm{Y} 1.400000 \mathrm{Z}-0.320088$
N632G0Z-0.1
N633G1X1.400000Y1.462500Z-0.1
N634G0Z-0. 321176
N635G1X1.400000Y1.400000Z-0.313304
N636G0Z-0.1
N637G1X1.275000Y1.525000Z-0.1
N638G0Z-0. 323486
N639G1X1.275000Y1.462500Z-0.314060 N640G0Z-0.1

N641G1X1.275000Y1.462500Z-0.1
N642G0Z-0. 314060
N643G1X1.275000Y1.400000Z-0.306520
N644G0Z-0.1
N645G1X1.150000Y1.462500Z-0.1
N646G0Z-0.307478
N647G1X1.150000Y1.400000Z-0.300245
N648GOZ-0.1
N649G1X1.025000Y1.462500Z-0.1
N650GOZ-0.301964
N651G1X1.025000Y1.400000Z-0.294988
N652G0Z-0.1
N653G1X0.900000Y1.462500Z-0.1
N654G0Z-0.298050
N655G1X0.900000Y1.400000Z-0.291256
N656G0Z-0.1
N657G1X0.775000Y1.462500Z-0.1
N658G0Z-0.296271
N659G1X0.775000Y1.400000Z-0.289560
N660G0Z-0.1
N661G1X0.650000Y1.462500Z-0.1
N662G0Z-0.297160
N663G1X0.650000Y1.400000Z-0.290408
N664G0Z-0.1
N665G1X0.650000Y1.025000Z-0.1
N666G0Z-0. 285344
N667G1X0.650000Y1.087500Z-0.281968
N668G0Z-0.1
N669G1X0.775000Y1.025000Z-0.1
N670G0Z-0. 284528
N671G1X0.775000Y1.087500Z-0.281172
N672G0Z-0.1
N673G1X0.900000Y1.025000Z-0.1
N674GOZ-0.286161
N675G1X0.900000Y1.087500Z-0.282765
N676G0Z-0.1
N677G1X1.025000Y1.025000Z-0.1
N678G0Z-0.289756
N679G1X1.025000Y1.087500Z-0.286268
N680G0Z-0.1
N681G1X1.150000Y1.025000Z-0.1
N682GOZ-0. 294820
N683G1X1.150000Y1.087500Z-0.291204
N684G0Z-0.1
N685G1X1.275000Y1.025000Z-0.1
N686G0Z-0.300865
N687G1X1.275000Y1.087500Z-0.297095
N688G0Z-0.1
N689G1X1.400000Y1.025000Z-0.1
N690G0Z-0.307400
N691G1X1.400000Y1.087500Z-0.303464
N692G0Z-0.1
N693G1X1.525000Y1.025000Z-0.1
N694G0Z-0.313935
N695G1X1. $525000 \mathrm{Y} 1.087500 \mathrm{Z}-0.309833$

N696G0Z-0.1
N697G1X1.650000Y1.087500Z-0.1
N698G0Z-0.315724
N699G1X1.650000Y1.150000Z-0.313597
N700G0Z-0.1
N701G1X1.775000Y1.087500Z-0.1
N702G0Z-0.320661
N703G1X1.775000Y1.150000Z-0.318468
N704G0Z-0.1
N705G1X1.900000Y1.087500Z-0.1
N706G0Z-0.324164
N707G1X1.900000Y1.150000Z-0.321926
N708G0Z-0.1
N709G1X1.900000Y1.400000Z-0.1
N710G0Z-0.335352
N711G1X1.900000Y1.337500Z-0.328639
N712G0Z-0.1
N713G1X1.775000Y1.400000Z-0.1
N714G0Z-0.331621
N715G1X1.775000Y1.337500Z-0.325045 N716G0Z-0.1
N717G1X1.650000Y1.400000Z-0.1
N718G0Z-0.326363
N719G1X1.650000Y1.337500Z-0.319980 N720G0Z-0.1

N721G1X1.525000Y1.400000Z-0.1
N722G0Z-0.320088
N723G1X1.525000Y1.337500Z-0.313935
N724G0Z-0.1
N725G1X1.400000Y1.400000Z-0.1
N726G0Z-0.313304
N727G1X1.400000Y1.337500Z-0.307400 N728G0Z-0.1
N729G1X1.275000Y1.400000Z-0.1
N730G0Z-0.306520
N731G1X1.275000Y1.337500Z-0.300865
N732G0Z-0.1
N733G1X1.150000Y1.400000Z-0.1
N734G0Z-0.300245
N735G1X1.150000Y1.337500Z-0.294820 N736G0Z-0.1
N737G1X1.025000Y1.400000Z-0.1
N738G0Z-0.294988
N739G1X1.025000Y1.337500Z-0.289756
N740G0Z-0.1
N741G1X0.900000Y1.400000Z-0.1
N742G0Z-0.291256
N743G1X0.900000Y1.337500Z-0.286161
N744G0Z-0.1
N745G1X0.775000Y1.400000Z-0.1
N746GOZ-0.289560
N747G1X0.775000Y1.337500Z-0.284528
N748G0Z-0.1
N749G1X0.775000Y1.087500Z-0.1
N750G0Z-0.281172

N751G1X0.775000Y1.150000Z-0.279495 N752G0Z-0.1
N753G1X0.900000Y1.087500Z-0.1
N754G0Z-0.282765
N755G1X0.900000Y1.150000Z-0.281066 N756G0Z-0.1
N757G1X1.025000Y1.087500Z-0.1
N758G0Z-0.286268
N759G1X1.025000Y1.150000Z-0.284524
N760G0Z-0.1
N761G1X1.150000Y1.087500Z-0.1
N762G0Z-0.291204
N763G1X1.150000Y1.150000Z-0.289395
N764G0Z-0.1
N765G1X1.275000Y1.087500Z-0.1
N766G0Z-0.297095
N767G1X1.275000Y1.150000Z-0.295210
N768G0Z-0.1
N769G1X1.400000Y1.087500Z-0.1
N770G0Z-0.303464
N771G1X1.400000Y1.150000Z-0.301496
N772G0Z-0.1
N773G1X1.525000Y1.150000Z-0.1
N774G0Z-0.307782
N775G1X1.525000Y1.212500Z-0.307782
N776G0Z-0.1
N777G1X1.650000Y1.150000Z-0.1
N778G0Z-0.313597
N779G1X1.650000Y1.212500Z-0.313597
N780G0Z-0.1
N781G1X1.775000Y1.1500002-0.1
N782G0Z-0.318468
N783G1X1.775000Y1.2125002-0.318469
N784G0Z-0.1
N785G1X1.775000Y1.337500Z-0.1
N786G0Z-0.325045
N787G1X1.775000Y1.275000Z-0.320661
N788G0Z-0.1
N789G1X1.650000Y1.337500Z-0.1
N790G0Z-0.319980
N791G1X1.650000Y1.275000Z-0.315724
N792G0Z-0.1
N793G1X1.525000Y1.337500Z-0.1
N794G0Z-0.313935
N795G1X1.525000Y1.275000Z-0.309833 N796G0Z-0.1
N797G1X1.400000Y1.337500Z-0.1
N798G0Z-0.307400
N799G1X1.400000Y1.275000Z-0.303464 N800G0Z-0.1
N801G1X1.275000Y1.3375002-0.1
N802G0Z-0.300865
N803G1X1.275000Y1.275000Z-0.297095 N804G0Z-0.1
N805G1X1.150000Y1.337500Z-0.1

N806G0Z-0.294820
N807G1X1.150000Y1.275000Z-0.291204
N808G0Z-0.1
N809G1X1.025000Y1.337500Z-0.1
N810G0Z-0.289756
N811G1X1.025000Y1.275000Z-0.286268
N812G0Z-0.1
N813G1X0.900000Y1.337500Z-0.1
N814G0Z-0. 286161
N815G1X0.900000Y1.275000Z-0.282765
N816G0Z-0.1
N817G1X0.900000Y1.150000Z-0.1
N818G0Z-0.281066
N819G1X0.900000Y1.212500Z-0.281066
N820G0Z-0.1
N821G1X1.025000Y1.150000Z-0.1
N822G0Z-0. 284524
N823G1X1.025000Y1.212500Z-0.284524
N824G0Z-0.1
N825G1X1.150000Y1.150000Z-0.1
N826G0Z-0.289395
N827G1X1.150000Y1.212500Z-0.289395
N828G0Z-0.1
N829G1X1.275000Y1.150000Z-0.1
N830G0Z-0.295210
N831G1X1.275000Y1.212500Z-0.295210
N832G0Z-0.1
N833G1X1.400000Y1.212500Z-0.1
N834G02-0. 301496
N835G1X1.400000Y1.2750002-0.303464
N836GOZ-0.1
N837G1X1.525000Y1.212500Z-0.1
N838G0Z-0.307782
N839G1X1.525000Y1.275000Z-0.309833
N840G0Z-0.1
N841G1X1.650000Y1.212500Z-0.1
N842G0Z-0. 313597
N843G1X1.650000Y1.275000Z-0.315724
N844G0Z-0.1
N845G1X1.650000Y1.275000Z-0.1
N846G0Z-0.315724
N847G1X1.650000Y1.212500Z-0.313597
N848G0Z-0.1
N849G1X1.525000Y1.275000Z-0.1
N850G0Z-0.309833
N851G1X1.525000Y1.212500Z-0.307782
N852G0Z-0.1
N853G1X1.400000Y1.275000Z-0.1
N854GOZ-0. 303464
N855G1X1.400000Y1.212500Z-0.301496
N856G0Z-0.1
N857G1X1.275000Y1.275000Z-0.1
N858G0Z-0. 297095
N859G1X1.275000Y1.212500Z-0.295210 N860G0Z-0.1

N861G1X1.150000Y1.275000Z-0.1
N862GOZ-0.291204
N863G1X1.150000Y1.212500Z-0.289395
N864G0Z-0.1
N865G1X1.025000Y1.275000Z-0.1
N866G0Z-0. 286268
N867G1X1.025000Y1.212500Z-0.284524
N868G0Z-0.1
N869G1X1.025000Y1.212500Z-0.1
N870G0Z-0.284524
N871G1X1.025000Y1.275000Z-0.286268
N872GOZ-0.1
N873G1X1.150000Y1.212500Z-0.1
N874GOZ-0. 289395
N875G1X1.150000Y1.275000Z-0.291204 N876G0Z-0.1
/* Start X zigzag machining */
N877G1X2.025000Y0.525000Z-0.1
N878G0Z-0.447708
N879G1X1.900000Y0.525000Z-0.444996 N880G0Z-0.1
N881G1X2.025000Y0.587500Z-0.1
N882G0Z-0.425124
N883G1X1.900000Y0.587500Z-0.422619
N884G0Z-0.1
N885G1X2.025000Y0.650000Z-0.1
N886G0Z-0.404799
N887G1X1.900000Y0.650000Z-0.402481
N888G0Z-0.1
N889G1X2.025000Y0.712500Z-0.1
N890GOZ-0. 386732
N891G1X1.900000Y0.712500Z-0.384580 N892G0Z-0.1
N893G1X2.025000Y0.775000Z-0.1
N894G0Z-0.370923
N895G1X1.900000Y0.775000Z-0.368916 N896G0Z-0.1
N897G1X2.025000Y0.837500Z-0.1
N898G0Z-0. 357373
N899G1X1.900000Y0.837500Z-0.355490 N900G0Z-0.1
N901G1X2.025000Y0.900000Z-0.1
N902G0Z-0.346081
N903G1X1.900000Y0.900000Z-0.344302
N904G0Z-0.1
N905G1X2.400000Y0.962500Z-0.1
N906GOZ-0.324837
N907G1X2.275000Y0.962500Z-0.332299 N908G0Z-0.1
N909G1X2.400000Y1.025000Z-0.1
N910G0Z-0.318510
N911G1X2.275000Y1.025000Z-0.325698 N912G0Z-0.1
N913G1X2.400000Y1.087500Z-0.1

N914G0Z-0.314292
N915G1X2.275000Y1.087500Z-0.321297
N916G0Z-0.1
N917G1X2.400000Y1.150000Z-0.1
N918G0Z-0.312182
N919G1X2.275000Y1.150000Z-0.319097
N920G0Z-0.1
N921G1X2.400000Y1.212500Z-0.1
N922G0Z-0. 312182
N923G1X2.275000Y1.212500Z-0.319097
N924G0Z-0.1
N925G1X2.400000Y1.275000Z-0.1
N926G0Z-0.314292
N927G1X2.275000Y1.275000Z-0.321297
N928G0Z-0.1
N929G1X2.400000Y1.337500Z-0.1
N930G0Z-0.318510
N931G1X2.275000Y1.337500Z-0.325698
N932G0Z-0.1
N933G1X2.400000Y1.400000Z-0.1
N934G0Z-0. 324837
N935G1X2.275000Y1.400000Z-0.332299
N936G0Z-0.1
N937G1X2.400000Y1.462500Z-0.1
N938G0Z-0.333273
N939G1X2.275000Y1.462500Z-0.341100
N940G0Z-0.1
N941G1X2.400000Y1.525000Z-0.1
N942G0Z-0.343818
N943G1X2.275000Y1.525000Z-0.352102
N944G0Z-0.1
N945G1X2.400000Y1.587500Z-0.1
N946G0Z-0.356472
N947G1X2.275000Y1.587500Z-0.365303
N948G0Z-0.1
N949G1X1.650000Y1.587500Z-0.1
N950G0Z-0.358279
N951G1X1.525000Y1.587500Z-0.350852
N952G0Z-0.1
N953G1X1.650000Y1.650000Z-0.1
N954G0Z-0.373173
N955G1X1.525000Y1.650000Z-0.365209
N956G0Z-0.1
N957G1X1.525000Y1.650000Z-0.1
N958G0Z-0.365209
N959G1X1.400000Y1.650000Z-0.356600
N960G0Z-0. 1
N961G1X1.525000Y1.712500Z-0.1
N962G0Z-0.381617
N963G1X1.400000Y1.712500Z-0.372344
N964G0Z-0.1
N965G1X1.400000Y1.7125002-0.1
N966G0Z-0. 372344
N967G1X1.275000Y1.712500Z-0.363071 N968G0Z-0.1

N969G1X1.400000Y1.775000Z-0.1 N970G0Z-0.390056
N971G1X1.275000Y1.775000Z-0.380037 N972G0Z-0.1
N973G1X1.275000Y1.775000Z-0.1
N974G0Z-0.380037
N975G1X1.400000Y1.775000Z-0. 390056
N976G0Z-0.1
N977G1X1.275000Y1.712500Z-0.1
N978G0Z-0.363071
N979G1X1.400000Y1.712500Z-0.372344
N980G0Z-0.1
N981G1X1.150000Y1.712500Z-0.1
N982G0Z-0.354494
N983G1X1.275000Y1.712500Z-0.363071
N984G0Z-0.1
N985G1X1.150000Y1.650000Z-0.1
N986G0Z-0.340028
N987G1X1.275000Y1.650000Z-0.347991
N988G0Z-0.1
N989G1X1.025000Y1.650000Z-0.1
N990G0Z-0.333356
N991G1X1.150000Y1.650000Z-0.340028
N992G0Z-0.1
N993G1X1.025000Y1.587500Z-0.1
N994G0Z-0.321148
N995G1X1.150000Y1.587500Z-0.327370
N996G0Z-0.1
N997G1X0.400000Y1.587500Z-0.1
N998GOZ-0. 329176
N999G1X0.525000Y1.587500Z-0.320345
N1000G0Z-0.1
N1001G1X0.400000Y1.525000Z-0.1
N1002G0Z-0.318214
N1003G1X0.525000Y1.525000Z-0.309931 N1004G0Z-0.1
N1005G1X0.400000Y1.462500Z-0.1
N1006G0Z-0. 309079
N1007G1X0.525000Y1.462500Z-0.301252
N1008G0Z-0.1
N1009G1X0.400000Y1.400000Z-0.1
N1010G0Z-0.301771
N1011G1X0.525000Y1.400000Z-0.294309
N1012G0Z-0.1
N1013G1X0.400000Y1.337500Z-0.1
N1014GOZ-0.296291
N1015G1X0.525000Y1.337500Z-0.289102
N1016G0Z-0.1
N1017G1X0.400000Y1.275000Z-0.1
N1018GOZ-0. 292637
N1019G1X0.525000Y1.275000Z-0.285631 N1020G0Z-0.1

N1021G1X0.400000Y1.212500Z-0.1
N1022G0Z-0.290810
N1023G1X0. $525000 \mathrm{Y} 1.212500 \mathrm{Z}-0.283895$

N1024G0Z-0.1
N1025G1X0.400000Y1.150000Z-0.1
N1026G0Z-0.290810
N1027G1X0.525000Y1.150000Z-0.283895
N1028G0Z-0.1
N1029G1X0.400000Y1.087500Z-0.1
N1030G0Z-0. 292637
N1031G1X0.525000Y1.087500Z-0.285631
N1032G0Z-0.1
N1033G1X0.400000Y1.025000Z-0.1
N1034G0Z-0.296291
N1035G1X0.525000Y1.025000Z-0.289102
N1036G0Z-0.1
N1037G1X0.400000Y0.962500Z-0.1
N1038G0Z-0.301771
N1039G1X0.525000Y0.962500Z-0.294309
N1040G0Z-0.1
N1041G1X1.525000Y0.900000Z-0.1
N1042G0Z-0.328292
N1043G1X1.650000Y0.900000Z-0.334874
N1044G0Z-0.1
N1045G1X1.525000Y0.837500Z-0.1
N1046G0Z-0.338547
N1047G1X1.650000Y0.837500Z-0.345512 N1048GOZ-0.1

N1049G1X1.525000Y0.775000Z-0.1
N1050G0Z-0.350852
N1051G1X1.650000Y0.775000Z-0.358279
N1052G0Z-0.1
N1053G1X1. $525000 \mathrm{Y} 0.712500 \mathrm{Z}-0.1$
N1054G0Z-0.365209
N1055G1X1.650000Y0.712500Z-0.373172
N1056G0Z-0.1
N1057G1X1.525000Y0.650000Z-0.1
N1058G0Z-0.381617
N1059G1X1.650000Y0.650000Z-0.390194
N1060G0Z-0.1
N1061G1X1.525000Y0.587500Z-0.1
N1062G0Z-0.400075
N1063G1X1.650000Y0.587500Z-0.409343
N1064G0Z-0.1
N1065G1X1.900000Y0.587500Z-0.1
N1066G0Z-0.422619
N1067G1X1.775000Y0.587500Z-0.417108
N1068G0Z-0.1
N1069G1X1.900000Y0.650000Z-0.1
N1070G0Z-0.402481
N1071G1X1.775000Y0.650000Z-0.397380
N1072G0Z-0.1
N1073G1X1.900000Y0.712500Z-0.1
N1074G0Z-0.384580
N1075G1X1.775000Y0.712500Z-0.379844
N1076G0Z-0.1
N1077G1X1.900000Y0.775000Z-0.1
N1078G0Z-0.368916

N1079G1X1.775000Y0.775000Z-0.364500 N1080G0Z-0.1
N1081G1X1.900000Y0.837500Z-0.1
N1082G0Z-0.355490
N1083G1X1.775000Y0.837500Z-0.351348 N1084G0Z-0.1
N1085G1X1.900000Y0.900000Z-0.1 N1086G0Z-0.344302
N1087G1X1.775000Y0.900000Z-0.340388 N1088G0Z-0.1
N1089G1X1.900000Y0.962500Z-0.1
N1090G0Z-0. 335352
N1091G1X1.775000Y0.962500Z-0.331620 N1092G0Z-0.1
N1093G1X2.275000Y1.025000Z-0.1
N1094GOZ-0. 325698
N1095G1X2.150000Y1.025000Z-0.329456
N1096GOZ-0.1
N1097G1X2.275000Y1.087500Z-0.1
N1098G0Z-0. 321297
N1099G1X2.150000Y1.087500Z-0.324960 N1100G0Z-0.1
N1101G1X2.275000Y1.150000Z-0.1
N1102GOZ-0.319097
N1103G1X2.150000Y1.150000Z-0.322712
N1104G0Z-0.1
N1105G1X2.275000Y1.212500Z-0.1
N1106G0Z-0.319097
N1107G1X2.150000Y1.212500Z-0.322712
N1108G0Z-0.1
N1109G1X2.275000Y1.275000Z-0.1
N1110G0Z-0.321297
N1111G1X2.150000Y1.275000Z-0.324960
N1112G0Z-0.1
N1113G1X2.275000Y1.337500Z-0.1
N1114G0Z-0.325698
N1115G1X2.150000Y1.337500Z-0.329456
N1116G0Z-0.1
N1117G1X2.275000Y1.400000Z-0.1
N1118G0Z-0.332299
N1119G1X2.150000Y1.400000Z-0.336200
N1120G0Z-0.1
N1121G1X2.275000Y1.462500Z-0.1
N1122G0Z-0.341100
N1123G1X2.150000Y1.462500Z-0.345192
N1124G0Z-0.1
N1125G1X2.275000Y1.525000Z-0.1
N1126G0Z-0.352102
N1127G1X2.150000Y1.525000Z-0.356432
N1128G0Z-0.1
N1129G1X1.525000Y1.525000Z-0.1
N1130G0Z-0. 338547
N1131G1X1.400000Y1.525000Z-0.331016 N1132G0Z-0.1
N1133G1X1.525000Y1.587500Z-0.1

N1134G0Z-0. 350852
N1135G1X1.400000Y1.587500Z-0.342824
N1136GOZ-0.1
N1137G1X1.400000Y1.587500Z-0.1
N1138GOZ-0.342824
N1139G1X1.275000Y1.587500Z-0.334796
N1140G0Z-0.1
N1141G1X1.400000Y1.650000Z-0.1
N1142G0Z-0.356600
N1143G1X1.275000Y1.650000Z-0.347991
N1144G0Z-0.1
N1145G1X1.275000Y1.650000Z-0.1
N1146G0Z-0.347991
N1147G1X1.400000Y1.650000Z-0.356600
N1148G0Z-0.1
N1149G1X1.275000Y1.587500Z-0.1
N1150G0Z-0.334796
N1151G1X1.400000Y1.587500Z-0.342824
N1152G0Z-0.1
N1153G1X1.150000Y1.587500Z-0.1
N1154G0Z-0. 327370
N1155G1X1.275000Y1.587500Z-0.334796
N1156G0Z-0.1
N1157G1X1.150000Y1.525000Z-0.1
N1158GOZ-0.316520
N1159G1X1.275000Y1.525000Z-0.323486
N1160G0Z-0.1
N1161G1X0.525000Y1.525000Z-0.1
N1162G0Z-0.309931
N1163G1X0.650000Y1.525000Z-0.305600
N1164G0Z-0.1
N1165G1X0.525000Y1.462500Z-0.1
N1166G0Z-0.301252
N1167G1X0.650000Y1.462500Z-0. 297160
N1168G0Z-0.1
N1169G1X0.525000Y1.400000Z-0.1
N1170G0Z-0. 294309
N1171G1X0.650000Y1.400000Z-0.290408 N1172G0Z-0.1
N1173G1X0.525000Y1.337500Z-0.1
N1174GOZ-0.289102
N1175G1X0.650000Y1.337500Z-0.285344
N1176G0Z-0.1
N1177G1X0.525000Y1.275000Z-0.1
N1178G0Z-0. 285631
N1179G1X0.650000Y1.275000Z-0.281968
N1180G0Z-0.1
N1181G1X0.525000Y1.212500Z-0.1
N1182G0Z-0.283895
N1183G1X0.650000Y1.212500Z-0.280280
N1184G0Z-0.1
N1185G1X0.525000Y1.150000Z-0.1
N1186G0Z-0. 283895
N1187G1X0.650000Y1.150000Z-0.280280 N1188G0Z-0.1

N1189G1X0.525000Y1.087500Z-0.1
N1190G0Z-0.285631
N1191G1X0.650000Y1.087500Z-0.281968 N1192G0Z-0.1
N1193G1X0. 525000Y1.025000Z-0.1
N1194G0Z-0.289102
N1195G1X0.650000Y1.025000Z-0.285344
N1196G0Z-0.1
N1197G1X1.650000Y0.962500Z-0.1
N1198G0Z-0.326363
N1199G1X1. $775000 \mathrm{Y} 0.962500 \mathrm{Z}-0.331620$
N1200G0Z-0.1
N1201G1X1.650000Y0.900000Z-0.1
N1202G0Z-0.334874
N1203G1X1.775000Y0.900000Z-0.340388 N1204G0Z-0.1
N1205G1X1.650000Y0.837500Z-0.1
N1206G0Z-0.345512
N1207G1X1. $775000 Y 0.837500 Z-0.351348$ N1208G0Z-0.1
N1209G1X1.650000Y0.775000Z-0.1
N1210G0Z-0.358279
N1211G1X1.775000Y0.775000Z-0.364500 N1212G0Z-0.1
N1213G1X1.650000Y0.712500Z-0.1
N1214G0Z-0.373172
N1215G1X1.775000Y0.712500Z-0.379844 N1216G0Z-0.1
N1217G1X1.650000Y0.650000Z-0.1
N1218G0Z-0.390194
N1219G1X1.775000Y0.650000Z-0.397380 N1220G0Z-0.1
N1221G1X1.775000Y0.650000Z-0.1
N1222G0Z-0.397380
N1223G1X1.650000Y0.650000Z-0.390194 N1224G0Z-0.1
N1225G1X1.775000Y0.712500Z-0.1
N1226G0Z-0.379844
N1227G1X1. $650000 Y 0.712500 \mathrm{Z}-0.373172$
N1228G0Z-0.1
N1229G1X1.775000Y0.775000Z-0.1
N1230G0Z-0. 364500
N1231G1X1.650000Y0.775000Z-0.358279
N1232G0Z-0.1
N1233G1X1. $775000 \mathrm{Y} 0.837500 \mathrm{Z}-0.1$
N1234G0Z-0. 351348
N1235G1X1.650000Y0.837500Z-0.345512 N1236G0Z-0.1
N1237G1X1.775000Y0.900000Z-0.1
N1238G0Z-0.340388
N1239G1X1. $650000 Y 0.900000 Z-0.334874$
N1240G0Z-0.1
N1241G1X1.775000Y0.962500Z-0.1
N1242G0Z-0.331620
N1243G1X1. $650000 \mathrm{Y} 0.962500 \mathrm{Z}-0.326363$

N1244G0Z-0. 1
N1245G1X1.775000Y1.025000Z-0.1
N1246G0Z-0. 325044
N1247G1X1.650000Y1.025000Z-0.319980
N1248G0Z-0.1
N1249G1X2.150000Y1.087500Z-0.1
N1250GOZ-0.324960
N1251G1X2.025000Y1.087500Z-0.325756
N1252G0Z-0. 1
N1253G1X2.150000Y1.150000Z-0.1
N1254G0Z-0. 322712
N1255G1X2.025000Y1.150000Z-0.323497
N1256G0Z-0.1
N1257G1X2.150000Y1.212500Z-0.1
N1258G0Z-0.322712
N1259G1X2.025000Y1.212500Z-0.323497
N1260GOZ-0.1
N1261G1X2.150000Y1.275000Z-0.1
N1262G0Z-0.324960
N1263G1X2.025000Y1.275000Z-0.325756
N1264GOZ-0.1
N1265G1X2.150000Y1.337500Z-0.1
N1266G0Z-0.329456
N1267G1X2.025000Y1.337500Z-0.330273
N1268G0Z-0.1
N1269G1X2.150000Y1.400000Z-0.1
N1270G0Z-0.336200
N1271G1X2.025000Y1.400000Z-0.337048
N1272G0Z-0.1
N1273G1X2.150000צ1.462500Z-0.1
N1274G0Z-0.345192
N1275G1X2.025000Y1.462500Z-0.346081 N1276G0Z-0.1
N1277G1X1.400000Y1.462500Z-0.1
N1278G0Z-0.321176
N1279G1X1.275000Y1.462500Z-0.314060 N1280G0Z-0.1
N1281G1X1.400000Y1.525000Z-0.1
N1282G0Z-0.331016
N1283G1X1.275000Y1.525000Z-0.323486 N1284G0Z-0.1
N1285G1X1.275000Y1.525000Z-0.1
N1286G0Z-0.323486
N1287G1X1.400000Y1.525000Z-0.331016
N1288G0Z-0.1
N1289G1X1.275000Y1.462500Z-0.1
N1290G0Z-0.314060
N1291G1X1.400000Y1.462500Z-0.321176
N1292G0Z-0.1
N1293G1X0.650000Y1.462500Z-0.1
N1294G0Z-0.297160
N1295G1X0.775000Y1.462500Z-0.296271
N1296G0Z-0.1
N1297G1X0.650000Y1.400000Z-0.1
N1298G0Z-0.290408

N1299G1X0.775000Y1.400000Z-0.289560 N1300G0Z-0.1
N1301G1X0.650000Y1.337500Z-0.1
N1302GOZ-0. 285344
N1303G1X0.775000Y1.337500Z-0.284528
N1304GOZ-0.1
N1305G1X0.650000Y1.275000Z-0.1
N1306GOZ-0. 281968
N1307G1X0.775000Y1.275000Z-0.281172
N1308G0Z-0.1
N1309G1X0.650000Y1.212500Z-0.1
N1310G0Z-0. 280280
N1311G1X0.775000Y1.212500Z-0.279495
N1312G0Z-0.1
N1313G1X0.650000Y1.150000Z-0.1
N1314G0Z-0. 280280
N1315G1X0.775000Y1.150000Z-0.279495 N1316G0Z-0.1
N1317G1X0.650000Y1.087500Z-0.1
N1318G0Z-0. 281968
N1319G1X0.775000Y1.087500Z-0.281172
N1320G0Z-0.1
N1321G1X1.650000Y1.087500Z-0.1
N1322GOZ-0.315724
N1323G1X1.525000Y1.087500Z-0.309833
N1324G0Z-0.1
N1325G1X2.025000Y1.150000Z-0.1
N1326G0Z-0. 323497
N1327G1X1.900000Y1.150000Z-0.321926
N1328G0Z-0.1
N1329G1X2.025000Y1.212500Z-0.1
N1330G0Z-0. 323497
N1331G1X1.900000Y1.212500Z-0.321926 N1332G0Z-0.1
N1333G1X2.025000Y1.275000Z-0.1
N1334G0Z-0. 325756
N1335G1X1.900000Y1.275000Z-0.324164
N1336G0Z-0.1
N1337G1X2.025000Y1.3375002-0.1
N1338GOZ-0.330273
N1339G1X1.900000Y1.337500Z-0.328639 N1340GOZ-0.1
N1341G1X2.025000Y1.400000Z-0.1
N1342G0Z-0. 337048
N1343G1X1.900000Y1.400000Z-0.335352
N1344G0Z-0.1
N1345G1X0.775000Y1.400000Z-0.1
N1346G0Z-0. 289560
N1347G1X0.900000Y1.400000Z-0.291256 N1348G0Z-0.1
N1349G1X0.775000Y1.337500Z-0.1
N1350G0Z-0.284528
N1351G1X0.900000Y1.337500Z-0.286161 N1352G0Z-0.1

N1353G1X0.775000Y1.275000Z-0.1
N1354G0Z-0. 281172
N1355G1X0.900000Y1.275000Z-0.282765
N1356G0Z-0.1
N1357G1X0.775000Y1.212500Z-0.1
N1358G0Z-0.279495
N1359G1X0.900000Y1.212500Z-0. 281066
N1360G0Z-0.1
N1361G1X0.775000Y1.150000Z-0.1
N1362GOZ-0. 279495
N1363G1X0.900000Y1.150000Z-0.281066
N1364G0Z-0.1
N1365G1X1.525000Y1.150000Z-0.1
N1366GOZ-0.307782
N1367G1X1.400000Y1.150000Z-0.301496
N1368GOZ-0.1
N1369G1X1.900000Y1.212500Z-0.1
N1370GOZ-0. 321926
N1371G1X1.775000Y1.212500Z-0.318469
N1372G02-0.1
N1373G1X1.900000Y1.275000Z-0.1
N1374GOZ-0.324164
N1375G1X1.775000Y1.275000Z-0.320661
N1376G0Z-0.1
N1377G1X1.900000Y1.337500Z-0.1
N1378G0Z-0.328639
N1379G1X1.775000Y1.337500Z-0.325045
N1380G0Z-0.1
N1381G1X0.900000Y1.337500Z-0.1
N1382G0Z-0. 286161
N1383G1X1.025000Y1.337500Z-0.289756 N1384G0Z-0.1
N1385G1X0.900000Y1.275000Z-0.1
N1386GOZ-0. 282765
N1387G1X1.025000Y1.2750002-0.286268 N1388G0Z-0.1
N1389G1X0.900000Y1.212500Z-0.1
N1390G0Z-0. 281066
N1391G1X1.025000Y1.212500Z-0.284524
N1392G0Z-0.1
N1393G1X1.400000Y1.212500Z-0.1
N1394G0Z-0. 301496
N1395G1X1.275000Y1.212500Z-0.295210
N1396G0Z-0.1
N1397G1X1.775000Y1.275000Z-0.1
N1398G0Z-0.320661
N1399G1X1.650000Y1.275000Z-0.315724
N1400GOZ-0.1
N1401G1X1.025000Y1.275000Z-0.1
N1402GOZ-0.286268
N1403G1X1.150000Y1.275000Z-0.291204
N1404G0Z0.5F3
N1405G1X0.0Y0.0
N1406M05

## REFERENCES

Beard, T. (1997), "Interpolating Curves," Modern Machine Shop, Oct, pp. 60-67.
Elber, G. and Cohen, E. (1994), "Toolpath Generation for Freeform Surface Models," Computer Aided Design, Vol. 26, No. 6, pp. 490-496.

Held, M., Lukacs, G., and Andor, L. (1994), "Pocket Machining Based on Contour-Parallel Tool Paths Generated by Means of Proximity Maps," Computer Aided Design, Vol. 26, No. 3, pp. 189-202.

Herrin, G. E. (1995), "CIM Perspectives," Modern Machine Shop, Sep, pp. 150-152.
Houtzeel, A. (1995), "A CAPP Perspective," Modern Machine Shop, Nov, pp. 72-79.
Hu, Y.N., Tse, W. C., Chen, Y. H., and Zhou, Z. D. (1998), "Tool -Path Planning for Rough Machining of a Cavity by Layer-Shape Analysis," International Journal of Advanced Manufacturing Technology, Vol. 14, pp. 321-329.

Jensen, C. G. and Anderson, D. C. (1996), "A Review of Numerically Controlled Methods for Finish-Sculptured-Surface Machining," IIE Transactions, Vol. 28, pp. 30-39.

Jeong, J. and Kim, K. (1998), "Tool Path Generation for Machining Free-Form Pockets Using Voronoi Diagrams," International Journal of Advanced Manufacturing Technology, Vol. 14, pp. 876-881.

Joo, J. and Cho, H. (1999), "Efficient Sculptured Pocket Machining Using Feature Extraction and Conversion," Journal of Manufacturing Systems, Vol. 18, No. 2, pp. 100-112.

Lee, Y. S. and Chang, T. C. (1995), "Application of Computational Geometry in Optimizing 2.5D and 3D NC Surface Machining," Computers in Industry, Vol. 26, pp. 41-59.

Lee, K. W., Kim, T. J., and Hong, S. E. (1994), "Generation of Toolpath with Selection of Proper Tools for Rough Cutting Process," Computer-Aided Design, Vol. 26, No. 11, pp. 822-831.

Lin, A. C. and Liu, H. T. (1998), "Automatic Generation of NC Cutter Path from Massive Data Points," Computer-Aided Design, Vol. 30, No. 1, pp. 77-90.

Lynch, M. (1996), "CNC Tech Talk," Modern Machine Shop, Apr, pp. 164-166.

Maeng, H.Y., Ly, M. H., and Vickers, G. W. (1996), "Feature-Based Machining of Curved Surfaces Using the Steepest Directed Tree Approach," Journal of Manufacturing System, Vol. 15, No. 6, pp. 379-391.

McLeod, R. J. Y. and Baart, M. L. (1998), " Geometry and Interpolation of Curves and Surfaces," Cambridge University Press.

O'Rourke, J. (1994), "Computational Geometry in C," Cambridge University Press.
Sarma, R. and Dutta, D. (1997), "The Geometry and Generation of NC Tool Paths," Journal of Mechanical Design, Vol. 119, Jun, pp. 253-258.

Suh, S. and Shin, Y. (1996), "Neural Network Modeling for Tool Path Planning of the Rough Cut in Complex Pocket Milling," Journal of Manufacturing Systems, Vol. 15, No. 5, pp. 295-304.

Vickers, G. W. and Bradley, C. (1992), "Curved Surface Machining through Circular Arc Interpolation," Computers in Industry, Vol.19, pp. 329-337.

Wang, H. P., Chang, H., and Wysk, R. A. (1988), "An Analytical Approach to Optimize NC Tool Path Planning for Face Milling Flat Convex Polygonal Surfaces," IIE Transactions, Sep, pp. 325-332.

Yang, D. and Kong, T. (1994), "Parametric Interpolator Versus Linear Interpolator for precision CNC Machining," Computer-Aided Design, Vol. 26, No. 3, pp. 225-234.

